

Diffractive Lepton-Hadron Scattering

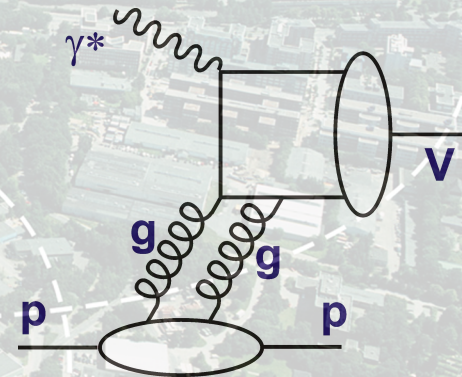
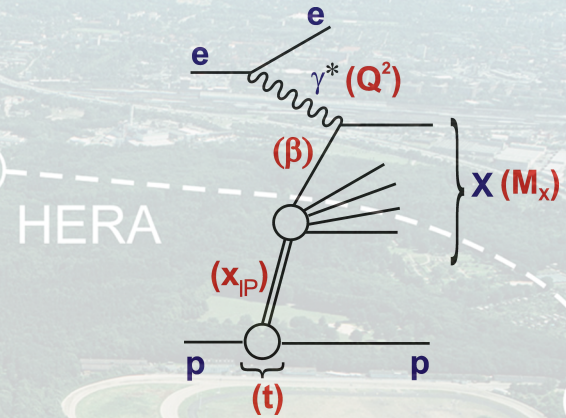
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Birmingham University



Cracow School of
Theoretical Physics:
'Electron-Ion Collider Physics'

Mon 20 September 2021

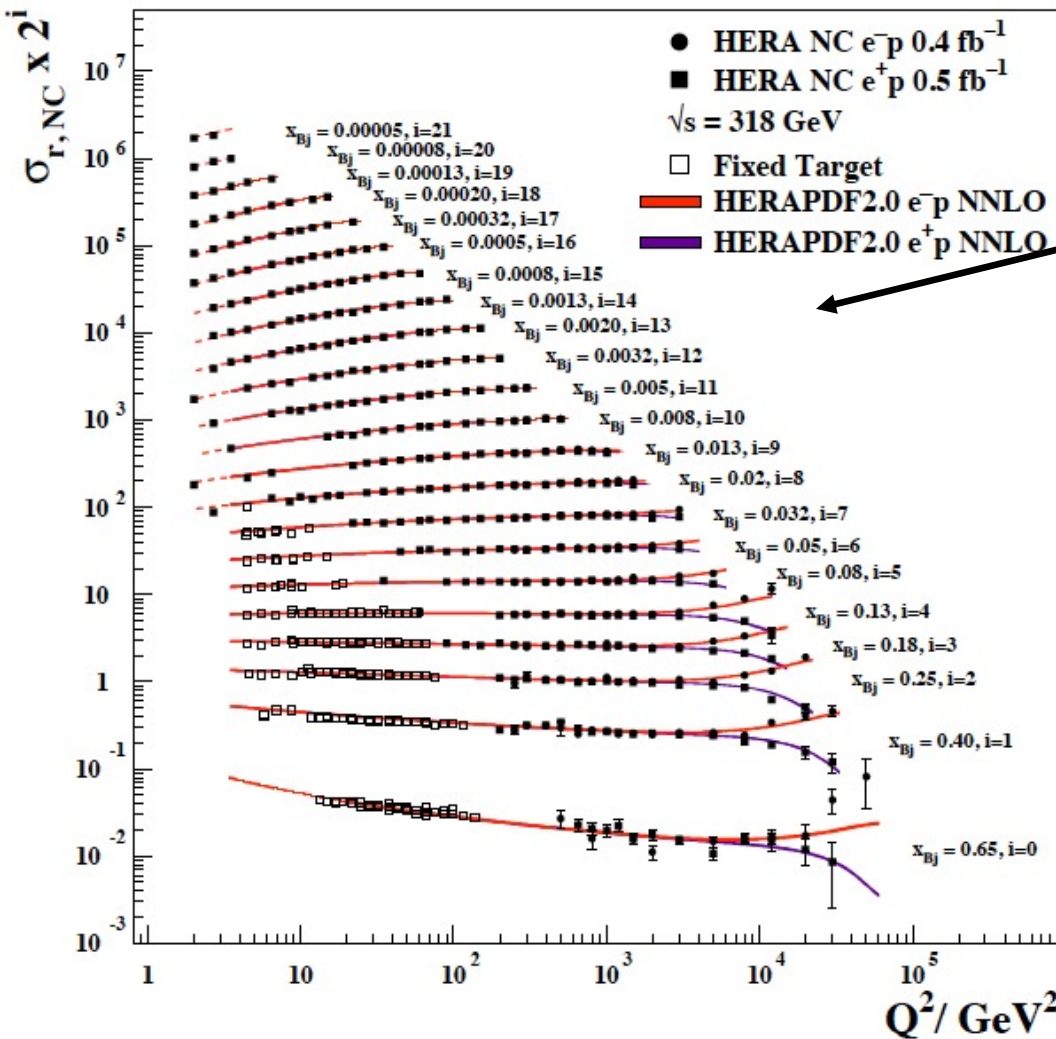
- 1) Introduction
- 2) Diffraction at HERA
- 3) Diffraction at the EIC



Low x Physics: A frontier of Standard Model

... HERA data as discussed by previous lecturer ...

H1 and ZEUS



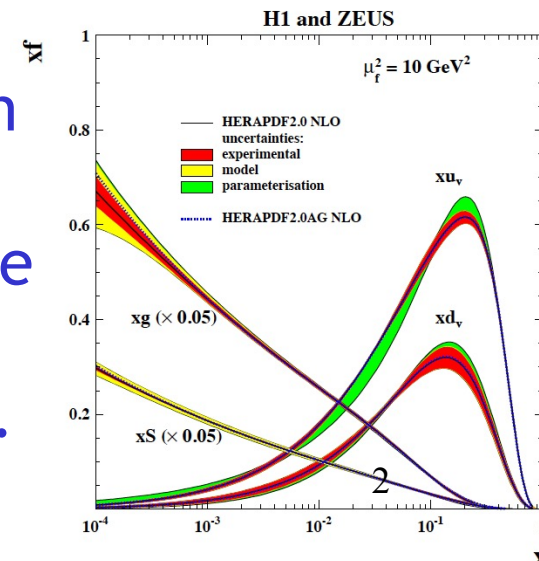
- NC Q^2 dependence in perturbative region driven by ...

$$g \rightarrow q\bar{q}$$

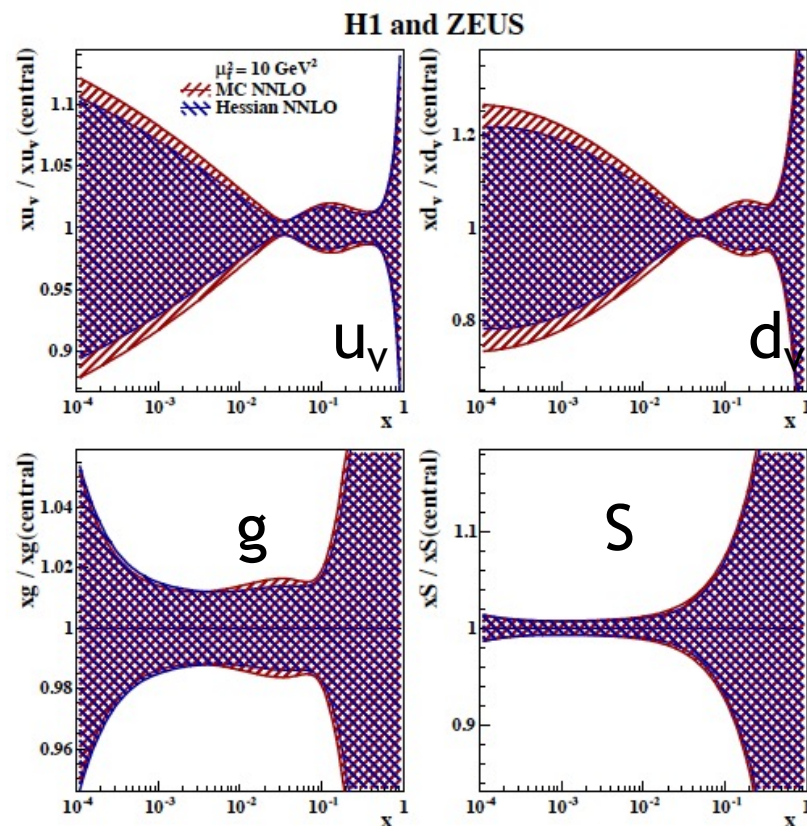
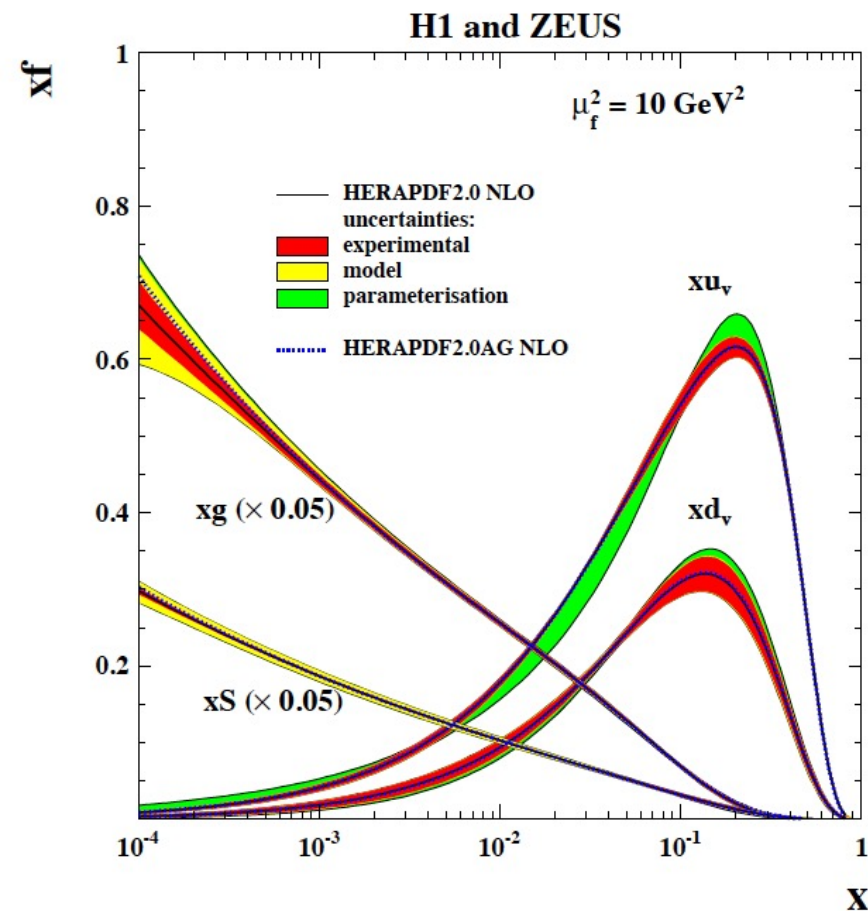
- e.g. Prytz approx:

$$\frac{dF_2(x, Q^2)}{d \ln Q^2} \sim G(2x)$$

- needs lever-arm in Q^2 ... reasonable precision to $x \sim 10^{-3}$.



Final HERA Picture of Proton (HERAPDF2.0)

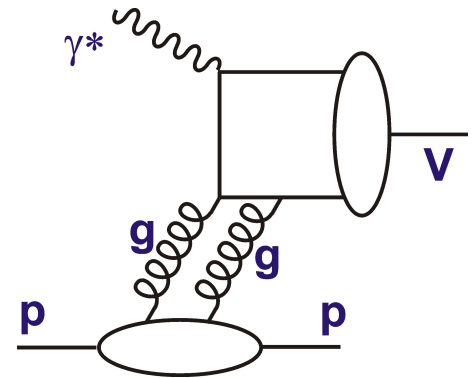


- ~2% precision on gluon over a wide range of x
- Gluon rises in a non-sustainable way ... **does it 'saturate'?**
- emergent phenomena at high parton density & strong coupling (including diffraction, non-linear evolution, confinement, mass ...)

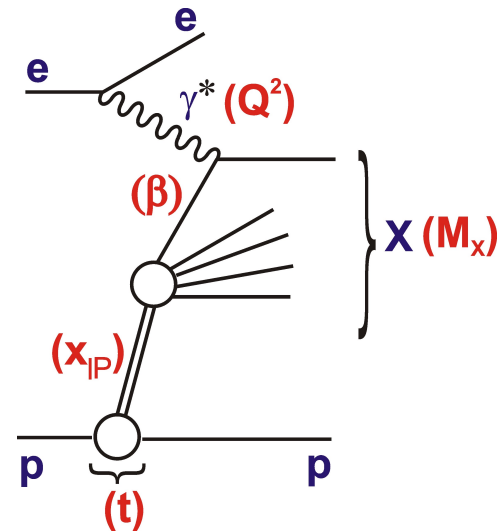
Exclusive / Diffractive Channels

- 1) [Low-Nussinov] interpretation as 2 gluon exchange enhances sensitivity to gluon density (at least for exclusives)
- 2) 2-parton correlations become accessible $\rightarrow$ 3D imaging!
- 3) New variable t gives access to impact parameter (b) dependent amplitudes

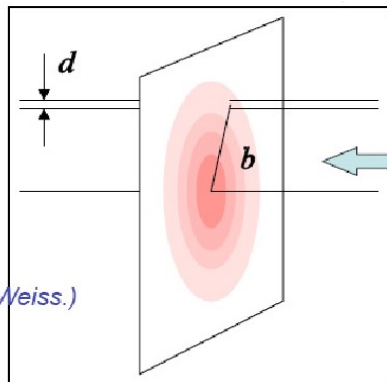
$\rightarrow$ Large t (small b) probes densest packed part of proton.



'Exclusive'



'Inclusive'

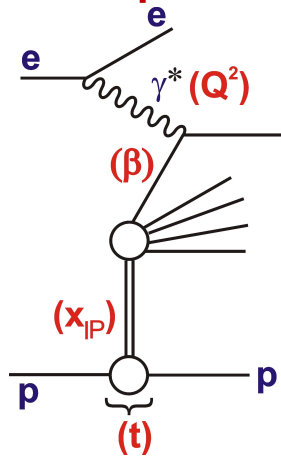


(figure from C. Weiss.)

Central black region growing with decrease of x .

Diffraction and HERA

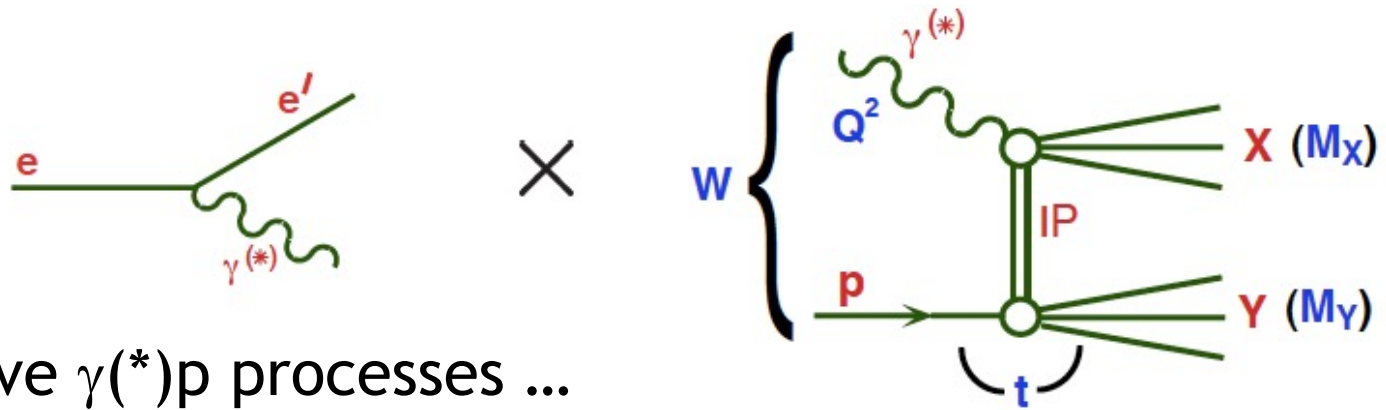
ep collisions
at $\sqrt{s} \sim 300 \text{ GeV}$
1992-2007
 $\sim 0.5 \text{ fb}^{-1}$ per expt.



e.g. H1 publications on diffraction (similar numbers in ZEUS):

- Inclusive diffractive cross sections: 15 papers
- Diffractive final states: 18 papers
- Quasi-elastic cross sections: 22 papers
- Total γp cross sections / decomposition: 2 papers

Diffractive Lepton-Hadron Scattering: Basics



Diffractive γ^*p processes ...

- HERA (and EIC) have favourable kinematics to study X system (photon dissociation)
- By varying Q^2 , the process can be smoothly changed
 - ... from a soft process (real photon, $Q^2 \rightarrow 0$)
 - ... to a deep inelastic process (highly virtual photon, large Q^2 , resolving partons and probing QCD structure)
- I will focus on cases where t is small

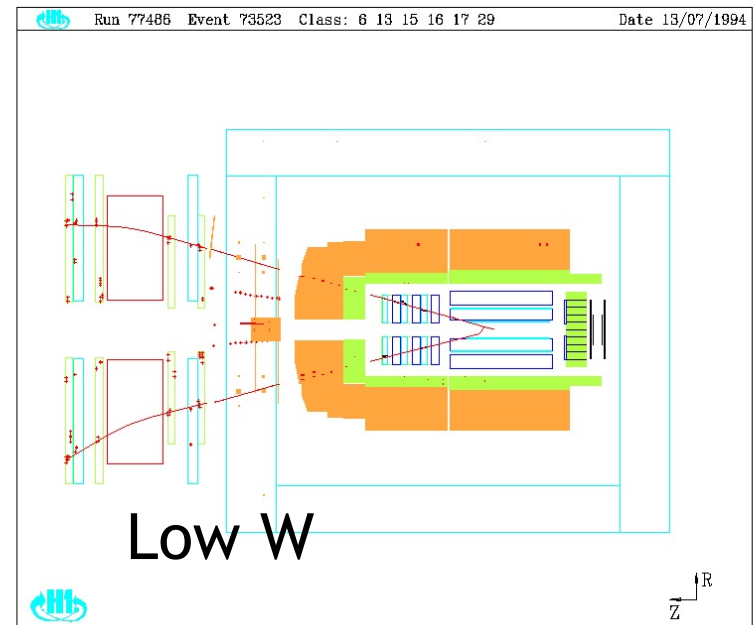
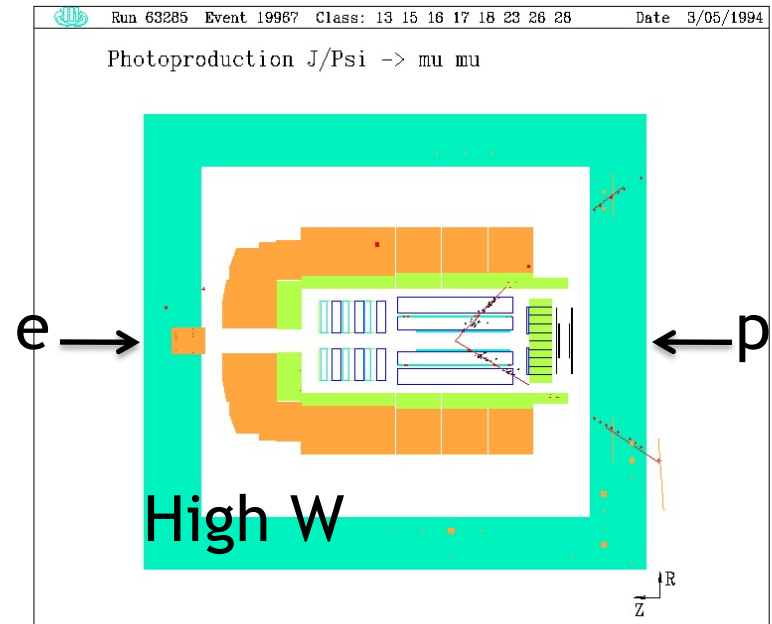
Exclusive Vector Meson Production

Experimental Selection (examples from H1 - Elastic $J/\Psi \rightarrow \mu\mu$)

2-prong decays give beautifully
clean events.

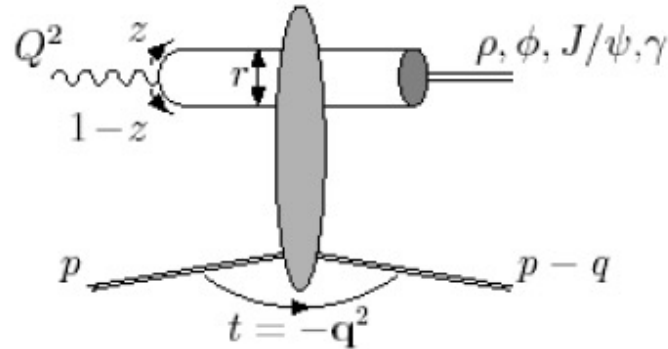
→ Select by requiring otherwise
empty detector

→ Decay muon direction is
determined by $W = \sqrt{s_{\gamma p}}$



Describing Vector Mesons in terms of Partons

Factorisation theorem



Dipole Models

step 1. γ fluctuation into $q \bar{q}$ dipole

step 2. dipole – proton interaction $A = \int dr^2 dz \Psi_\gamma \sigma(\text{dip} - p) \Psi_V$

step 3. pair recombination into VM

1. γ wave function

well known : $\Psi(z, k_t)$

however : large $|t|$ studies $\rightarrow$ chiral odd contributions

- Basically known

3. pair recombination into VM

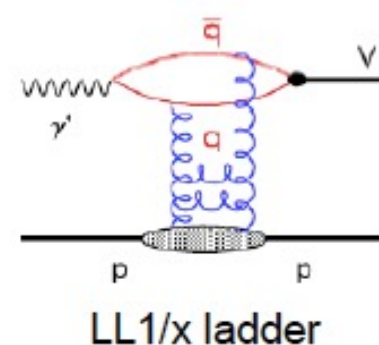
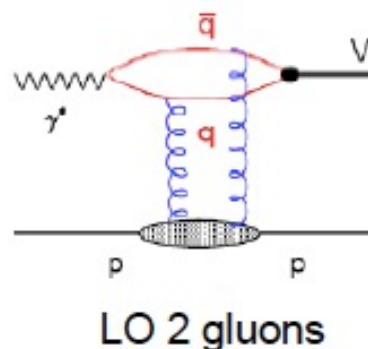
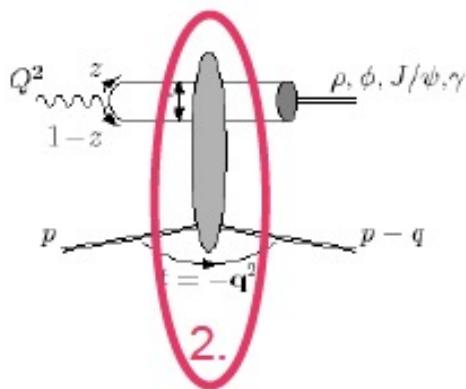
- VM wave function description ?

- role on σ_L / σ_T and helicity amplitudes

- Limits theoretical precision

The Dipole-Proton Interaction

2. dipole – proton interaction - The interesting physics



VM production is a promising candidate to learn about the gluon distribution in hadrons and the correlations among gluons

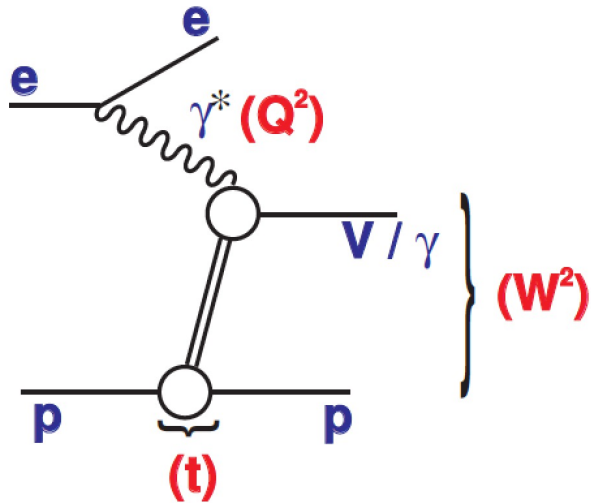
Many models on the details of $\sigma(r)$ (see later talks)

What is the relevant scale?... r depends on Q^2 and M_V^2

$$Q_{\text{eff}}^2 = z (1-z) (Q^2 + M_V^2) \sim (Q^2 + M_V^2) / 4$$

[MRT¹⁰.]

Vector Mesons & the Soft $\rightarrow$ Hard Transition



Behaviour usually parameterised in Regge-theory motivated form

$$\frac{d\sigma_{el}}{dt} \sim \left(\frac{W^2}{W_0^2} \right)^{2\alpha(t)-2} e^{bt}$$

- $\alpha(t) = \alpha(0) + \alpha' t$ is the ‘effective pomeron trajectory’
 ‘Universal’ description of soft physics: $\alpha(t) \sim 1.08 + 0.25t$
- e^{bt} empirically motivated - Fourier transform of spatial distribution of interaction
 $b = b_{\text{dipole}} + b_{\text{proton}} \rightarrow b_{\text{proton}}$ as dipole size $\rightarrow 0$
- Signatures for ‘hard’ behaviour include increase in $\alpha(0)$ and decrease in b

Photoproduction of Light v Heavy VM

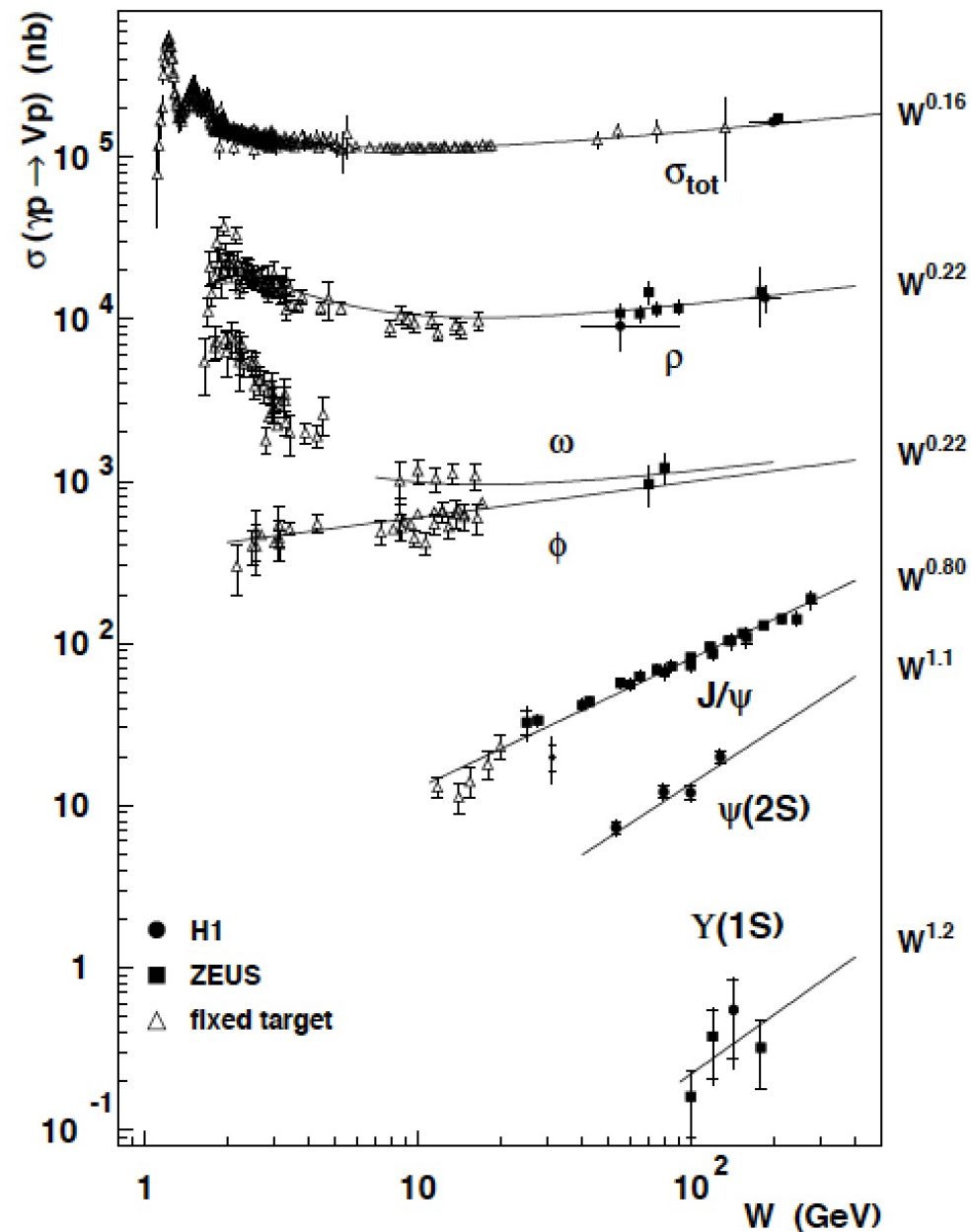
Increasing M_V leads to harder energy dependences

$$\sigma \propto W^\delta \text{ with } \delta = 4\alpha(\langle t \rangle) - 4$$

- Consistent with soft pomeron for light vector mesons

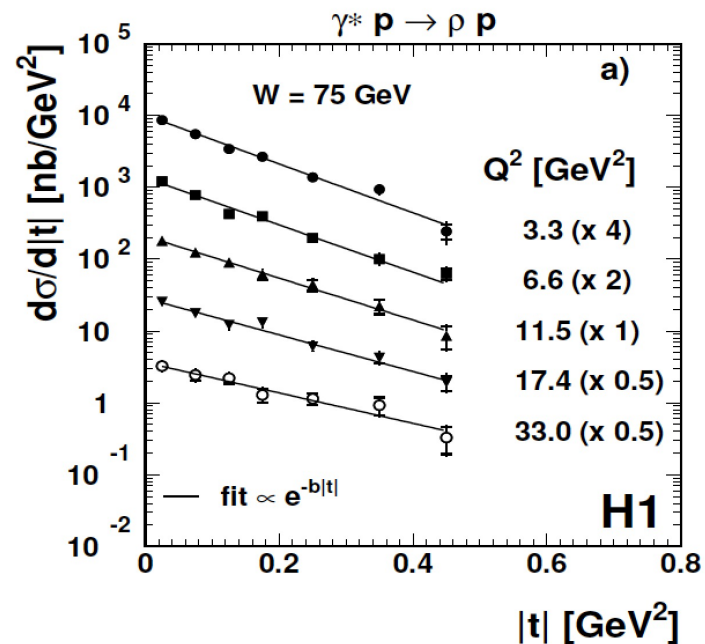
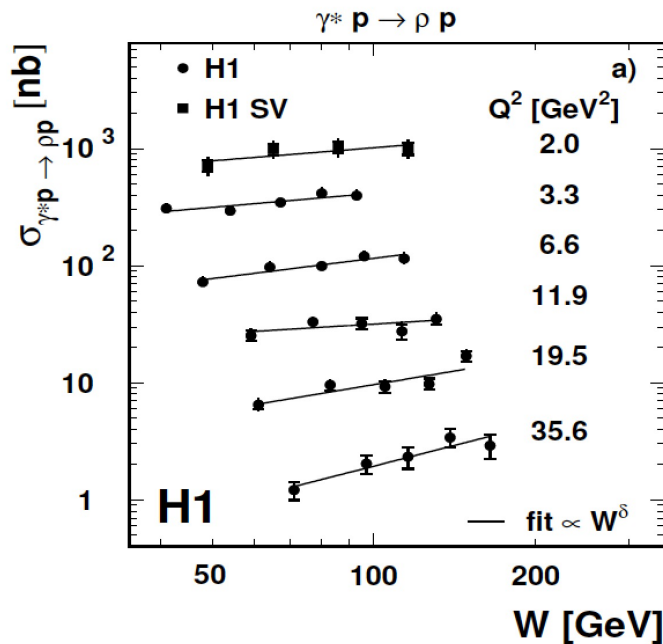
- For J/Ψ , effective $\alpha(t) \sim 1.20 + 0.13t$

... c, b mass implies pQCD already valid for J/Ψ , Y at $Q^2 = 0$



Turning the Q^2 Handle

- J/Ψ : W & t dependences $\sim$ unchanged - already hard @ $Q^2=0$
- Light vector meson behaviour evolves from soft to hard (eg ρ^0)

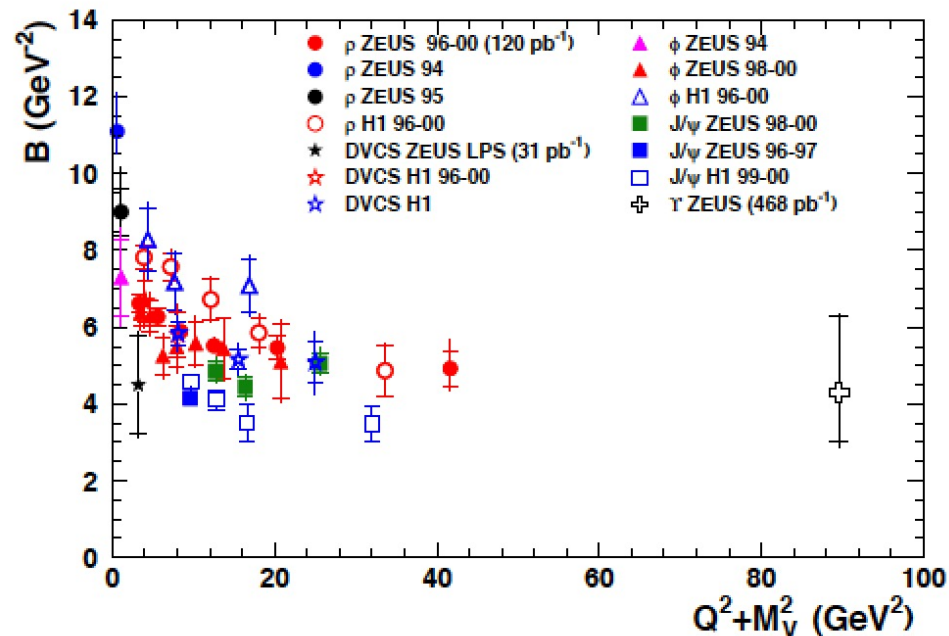
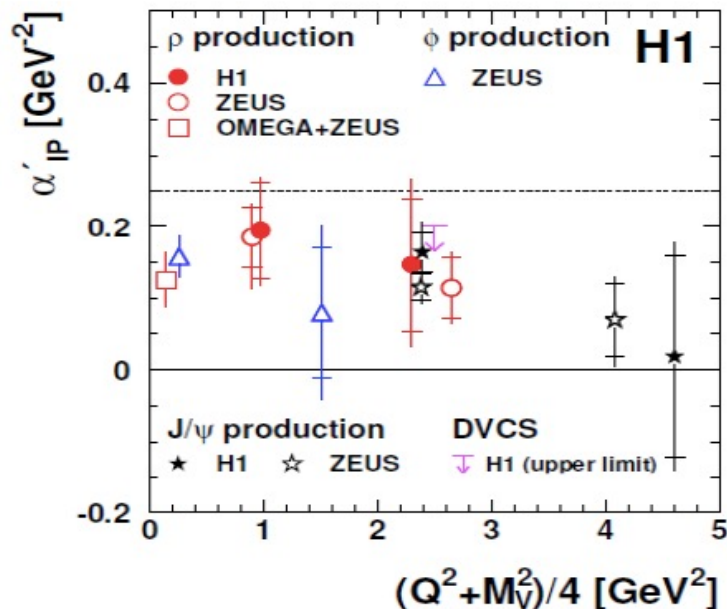
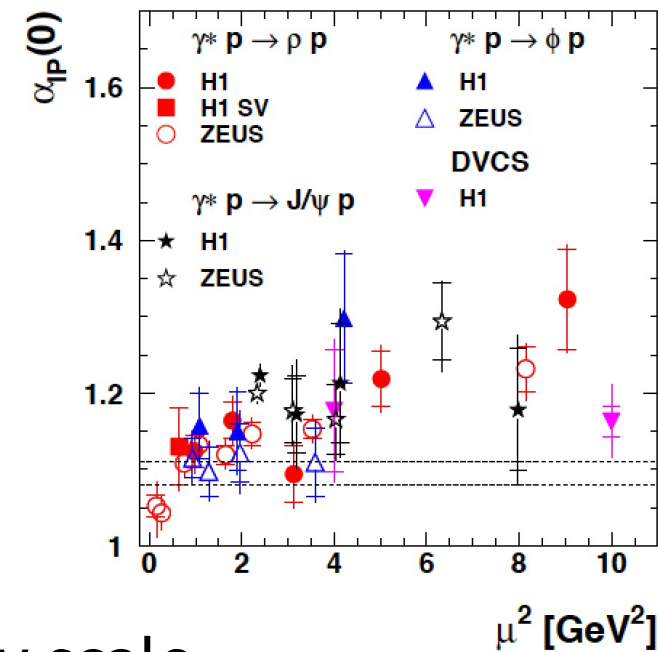


- Vector mesons produced from longitudinal and transverse polarised photons behave slightly differently
- Fast reduction in cross section with Q^2 illustrates higher twist nature of process: $\sigma_L \sim 1/(Q^2 + M_V^2)^{2.1}$, $\sigma_T \sim 1/(Q^2 + M_V^2)^{2.9}$
- ... reasonably well described by dipole (2 gluon) models

VM Overall

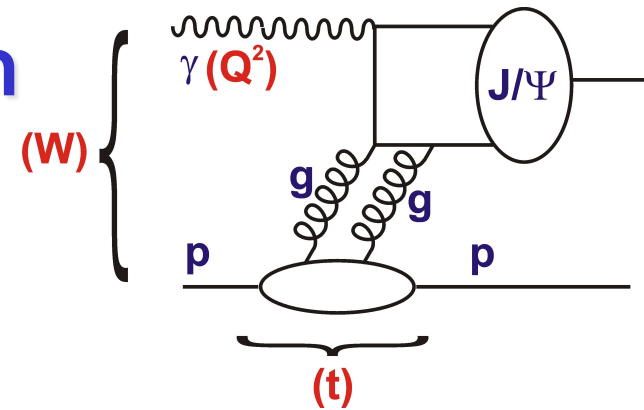
Characterisation Summary

- Approximate scaling between different meson species in $(Q^2 + M_V^2)/4$
- t-slope approaches $B \sim 4\text{-}5 \text{ GeV}^{-2} \sim 0.6\text{fm}$
... slightly smaller than EM size of proton?
- α' shows no significant variation with any scale.



Exclusive J/Ψ Photoproduction

Maybe the ideal place to look for gluon saturation in ep, eA ...



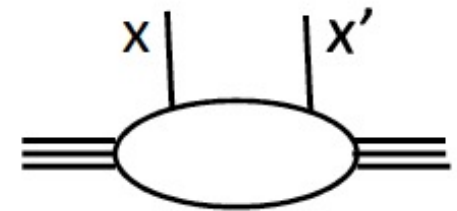
Advantages

- Clean 2 lepton experimental signature
- Scale $\bar{Q}^2 \sim (Q^2 + M_V^2)/4 > \sim 3 \text{ GeV}^2$ ideally suited to reaching lowest possible x whilst in perturbative regime

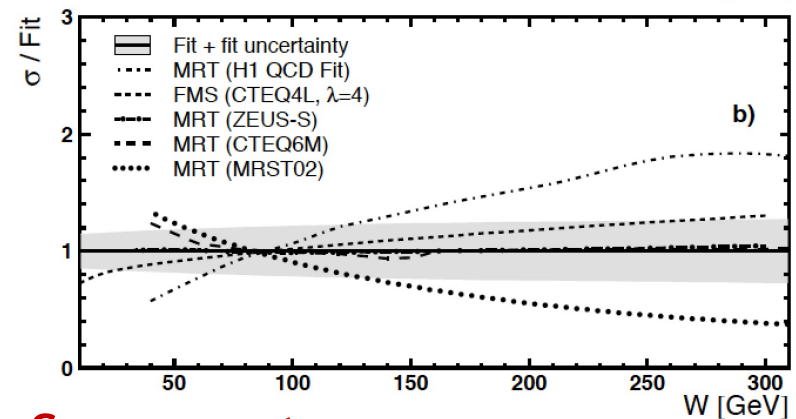
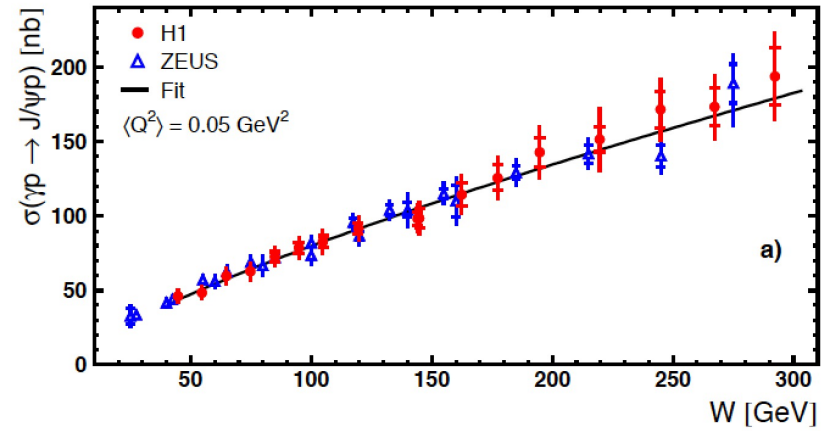
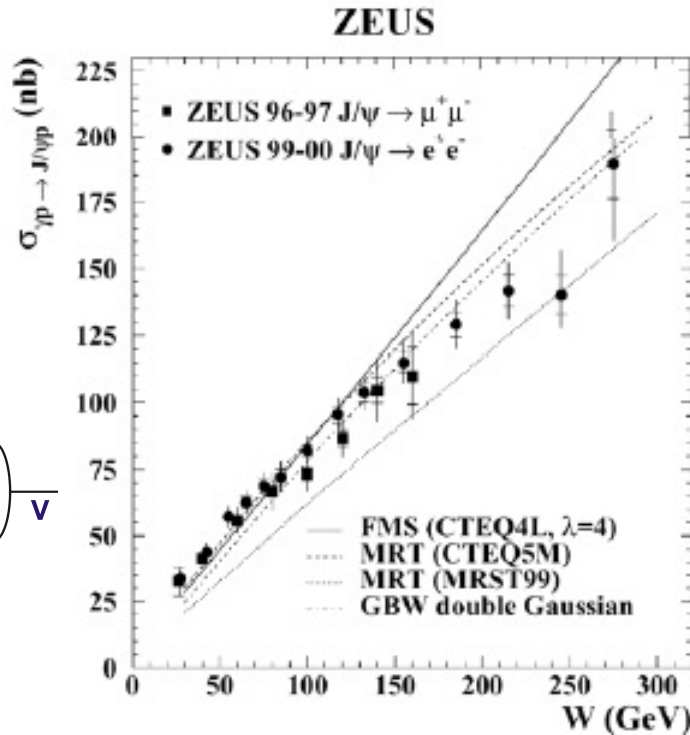
Possible clear saturation signature: energy (W) dependence flattening in a manner dependent on t or in eA as A grows

Complications

- Vector meson wavefunction
- Difficulties in collinear factorization theory $\rightarrow$ large scale uncertainties (NLO v LO convergence)



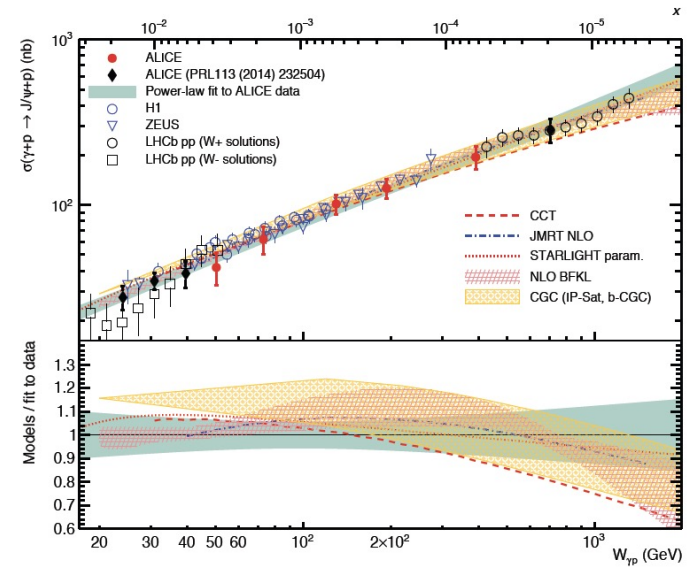
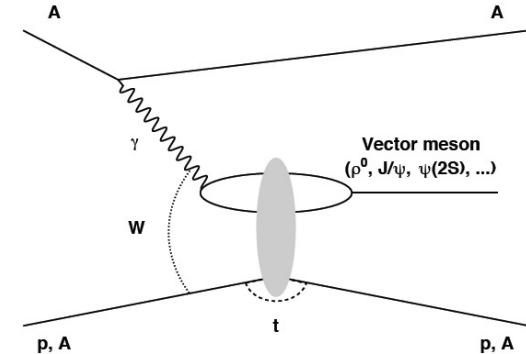
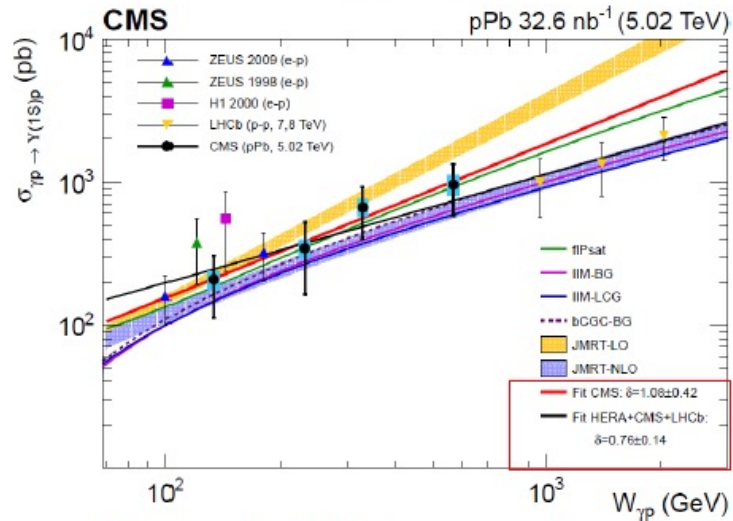
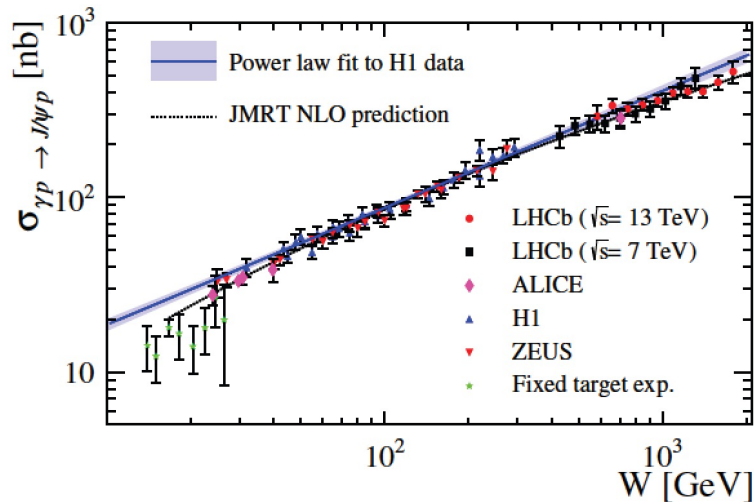
HERA Photoproduction of J/ψ and the Gluon



- QCD models based on 2-gluon exchange describe HERA data well & suggest power to discriminate between PDFs
- Sensitivity limited by theory uncertainties
- No evidence for saturation phenomena in HERA data (all ep)

Exclusive J/Ψ Data from the LHC

J/Ψ Photoproduction also studied (at higher energy)
in Ultraperipheral Collisions at LHC



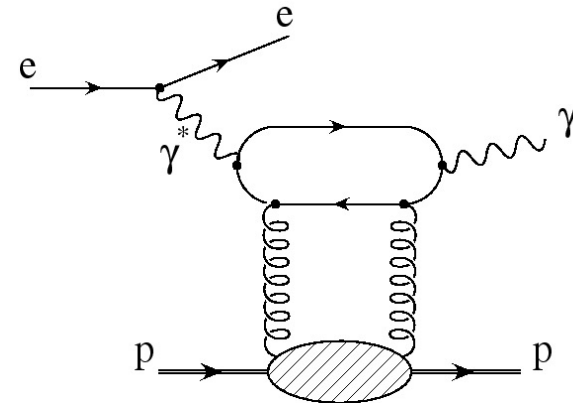
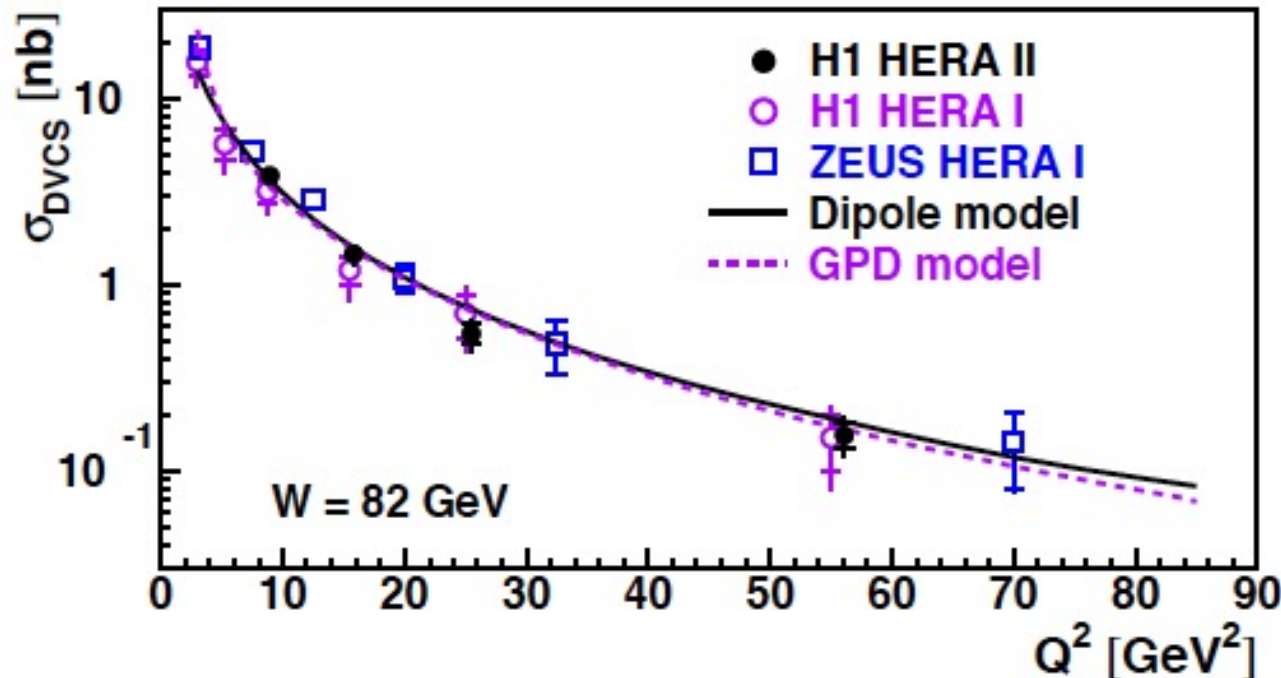
- No sign of deviation from simple power law behaviour (yet)
- More subtle signatures may exist in t dependences and eA/ep

Deeply Virtual Compton Scattering ($ep \rightarrow e\gamma p$)

- DVCS is the classic exclusive process to investigate hadron transverse structure and correlations via Generalised Parton Densities

... BUT ...

- HERA measurements were luminosity-limited (lower cross sections than Vector Mesons due to γ coupling)
- HERA did not have polarised proton beams

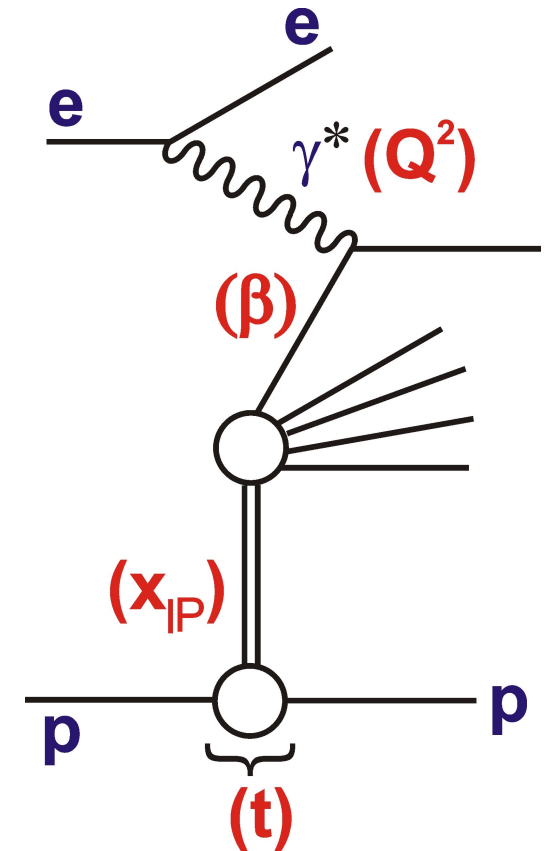
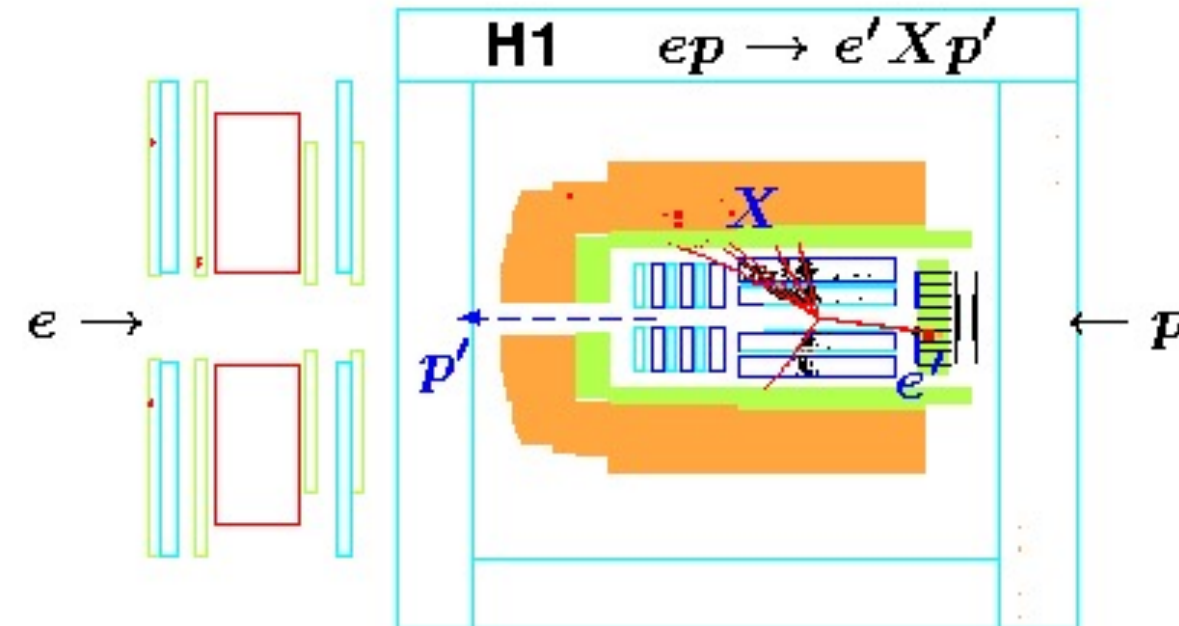


Inclusive Diffraction in Deep Inelastic Scattering

Diffractive DIS

Vector meson production is a 'higher twist' (Q^2 suppressed) process

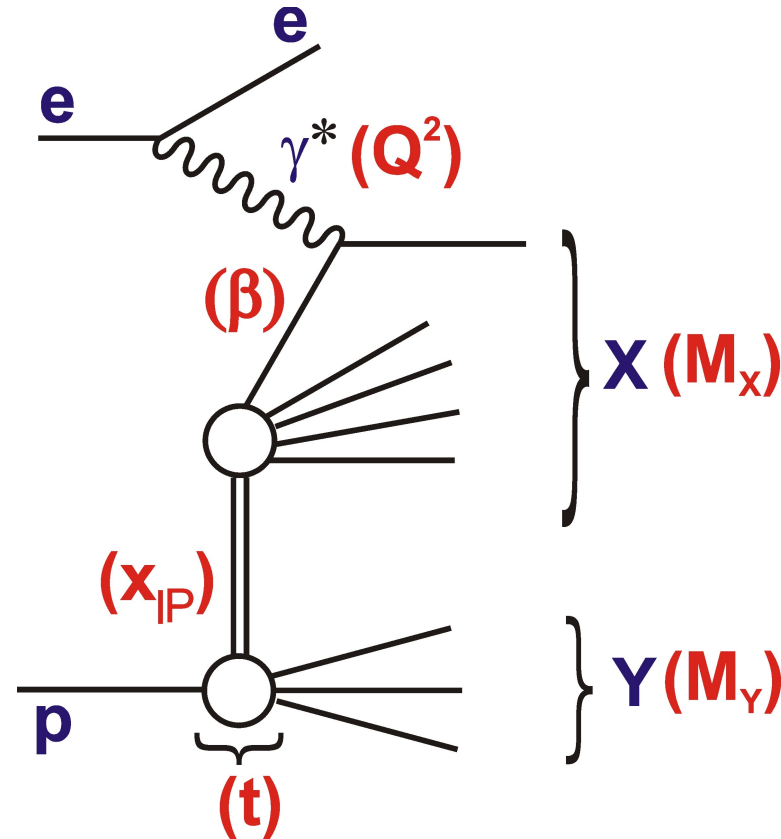
There are 'leading twist' diffractive processes with same Q^2 dependence as the bulk DIS cross section ...



~10% of DIS events have no forward energy flow

Kinematics

Most generally $ep \rightarrow eXY \dots$



In most cases here, $Y=p$,
(small admixture of low
mass excitations)

Standard DIS variables ...

x = momentum fraction q/p

$Q^2 = |\gamma^* \text{ 4-momentum squared}|$

Additional variables
for diffraction ...

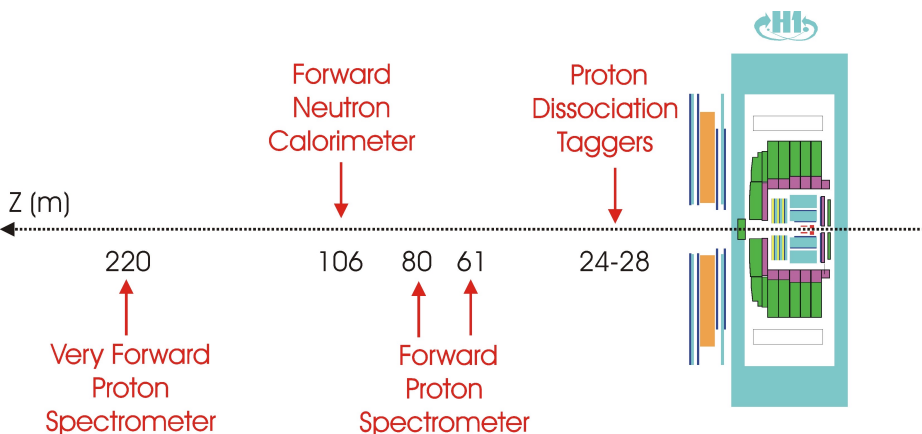
t = squared 4-momentum
transfer at proton vertex

x_{IP} = fractional momentum
loss of proton
(momentum fraction IP/p)

$\beta = x / x_{IP}$
(momentum fraction q / IP)

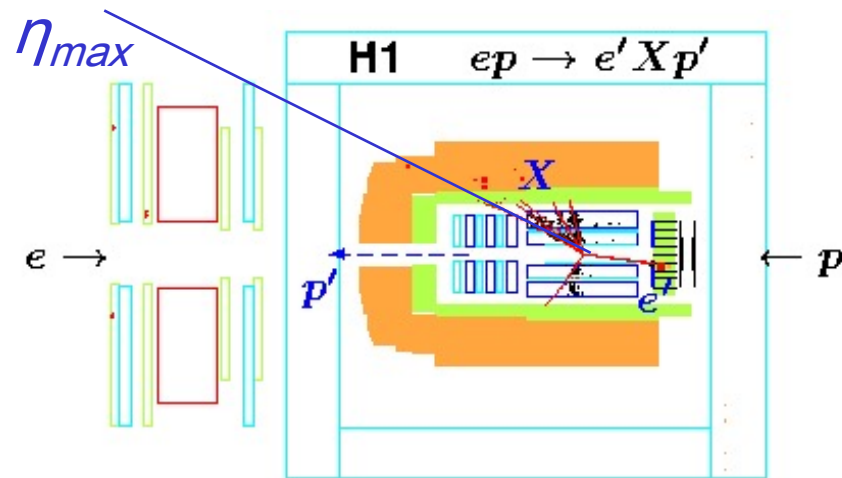
Signatures and Selection Methods

Scattered proton in Leading Proton Spectrometers (LPS)



Limited by statistics and p-tagging systematics

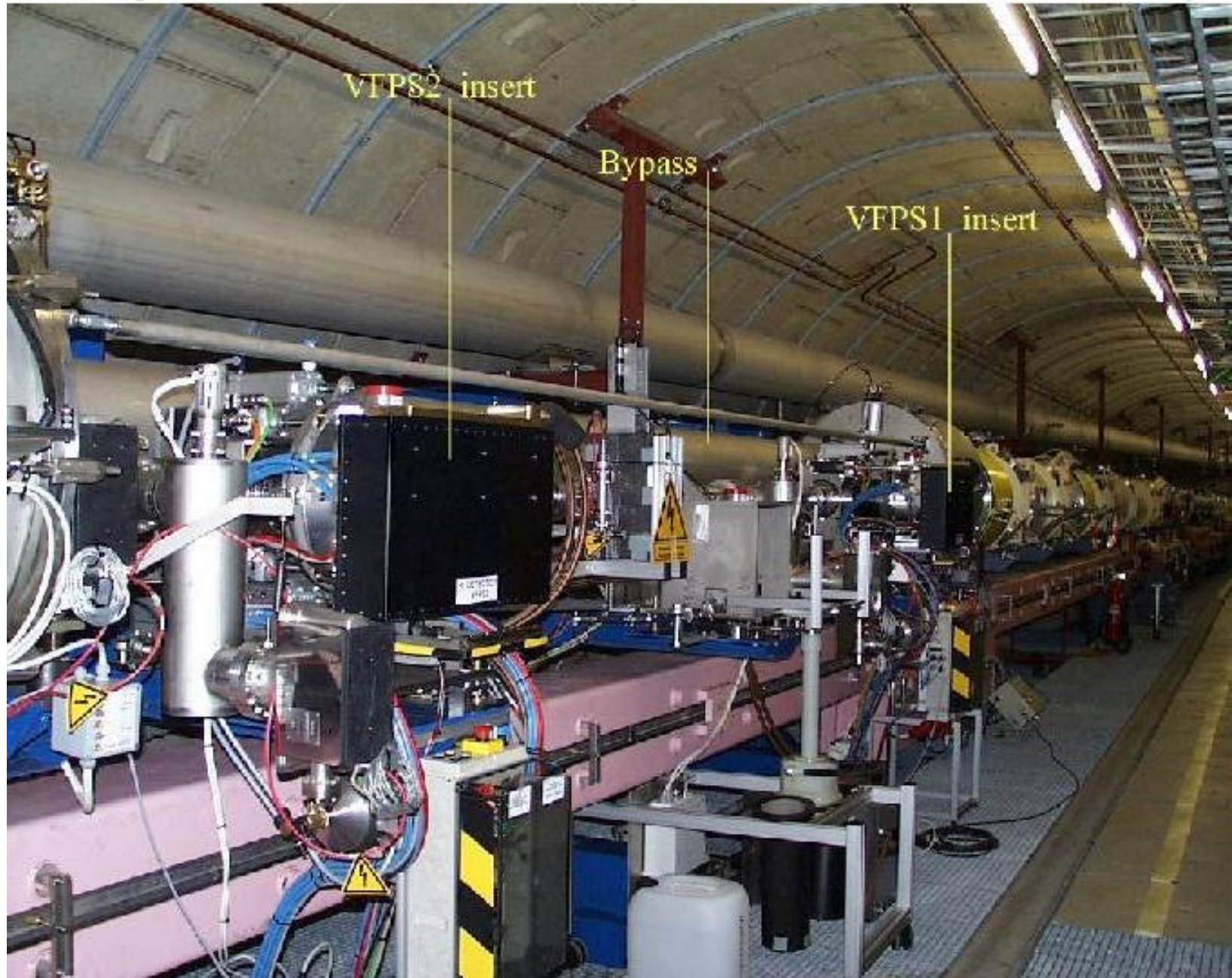
'Large Rapidity Gap' (LRG) adjacent to outgoing (untagged) proton



Limited by p-diss systematics

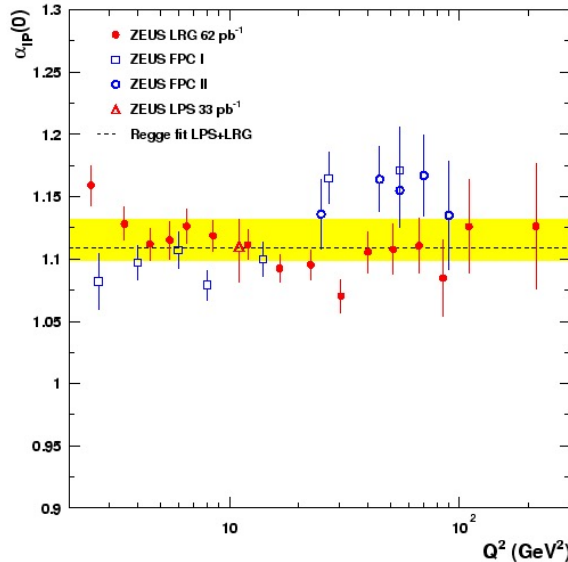
- The 2 methods have very different systematics
- LRG was the main method used at HERA
- At EIC it is more likely to be LPS (technologies improved!)

Example Roman Pots (H1 VFPS @ ~200m)

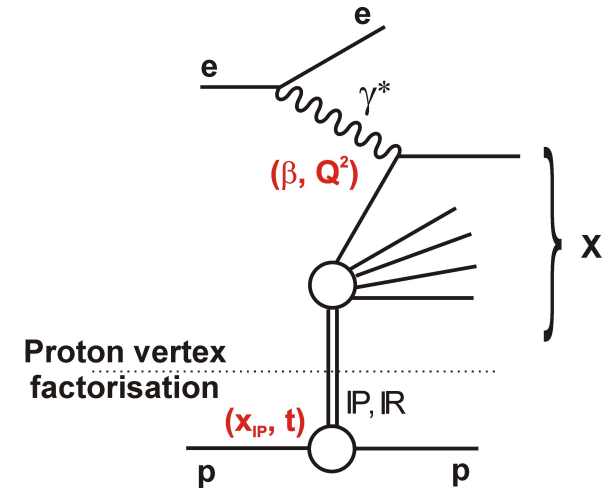
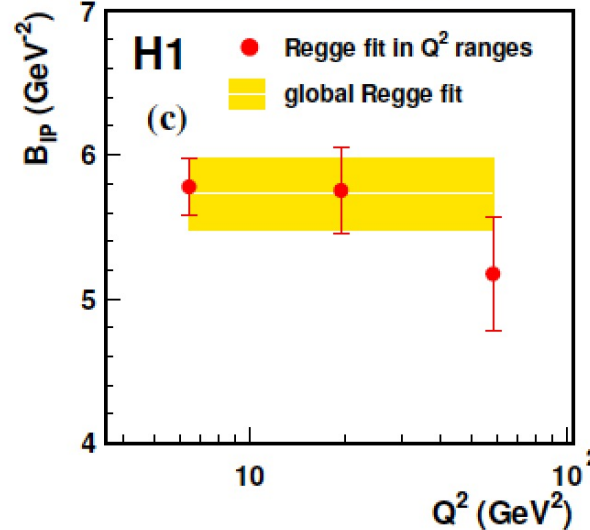


Proton Vertex Factorisation & the Effective Pomeron of Diffractive DIS

ZEUS



H1 FPS HERA II



- x_{IP} (via $\alpha_{IP}(0)$) and t (via b slope) dependence invariant with Q^2 and β !

$$\alpha_{IP}(0) = 1.10 \pm 0.02 \text{ (exp.)} \pm 0.03 \text{ (model)}$$

e.g. From H1 FPS data: $\alpha'_{IP} = 0.04 \pm 0.02 \text{ (exp.)} \pm 0.07 \text{ (model)} \text{ GeV}^{-2}$

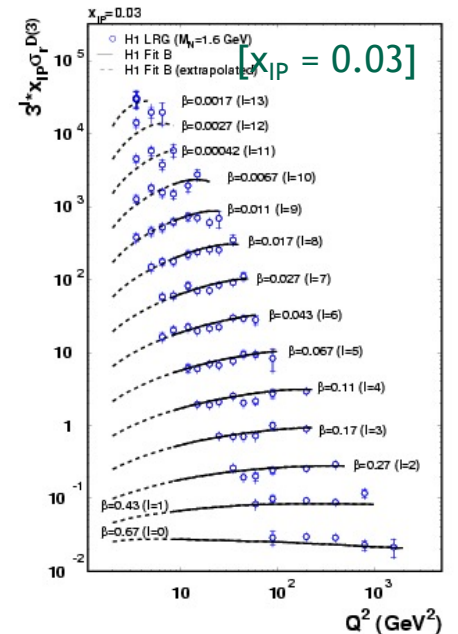
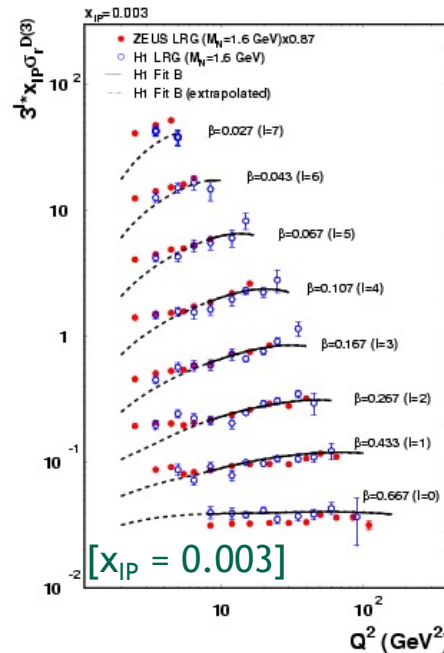
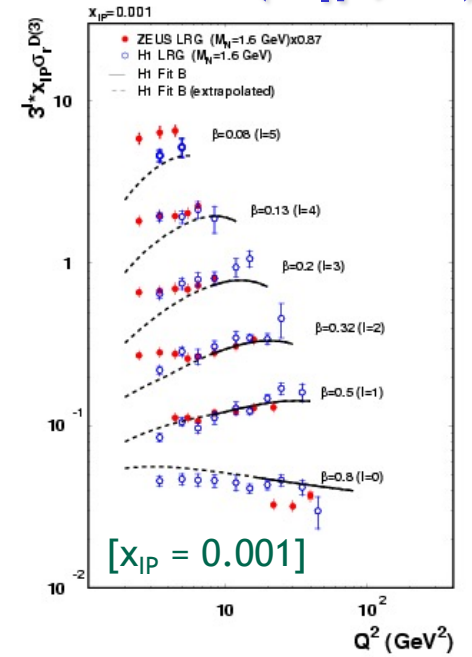
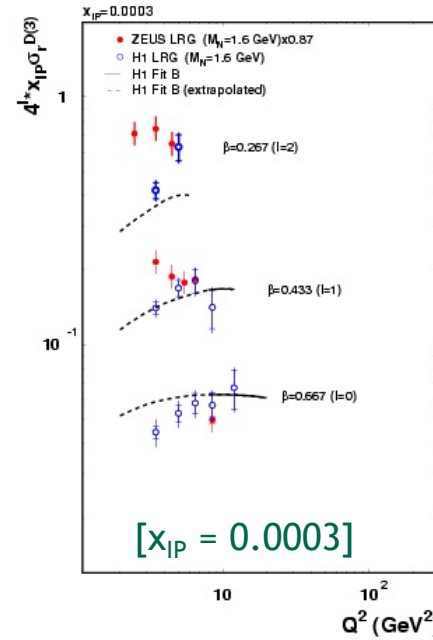
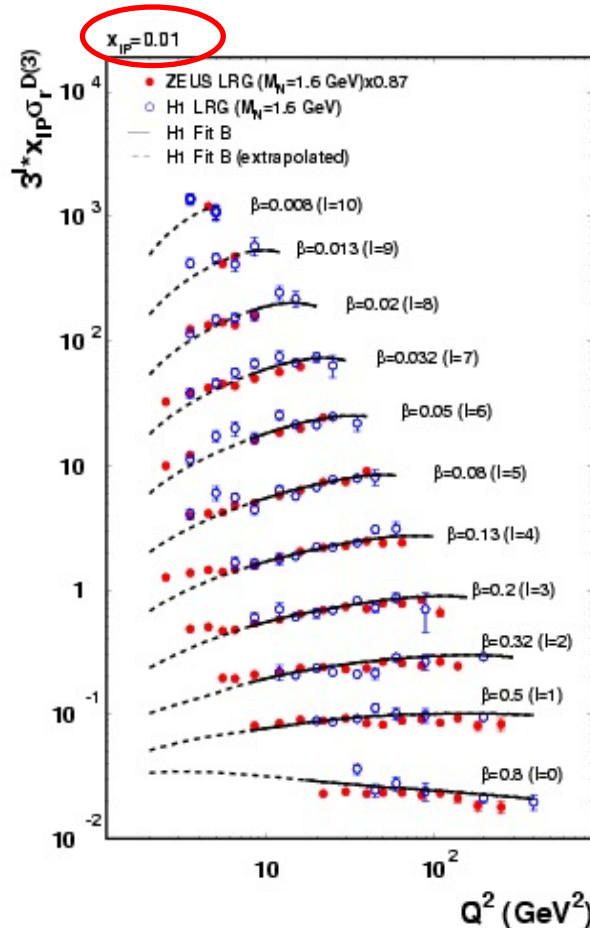
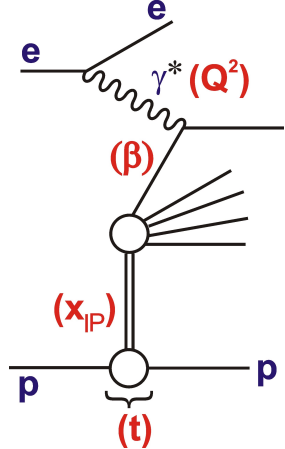
$$B_{IP} = 5.7 \pm 0.3 \text{ (exp.)} \pm 0.9 \text{ (model)} \text{ GeV}^{-2}$$

$\alpha_{IP}(0)$ consistent with soft IP
 α_{IP}' smaller than soft IP

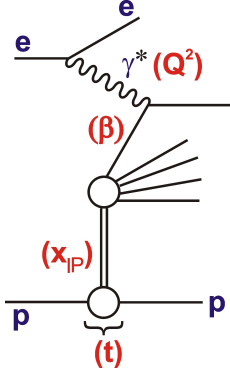
→ Dominantly soft exchange
 → Absorptive effects?...²⁴

(β, Q^2) Dependences at fixed (x_{IP}, t)

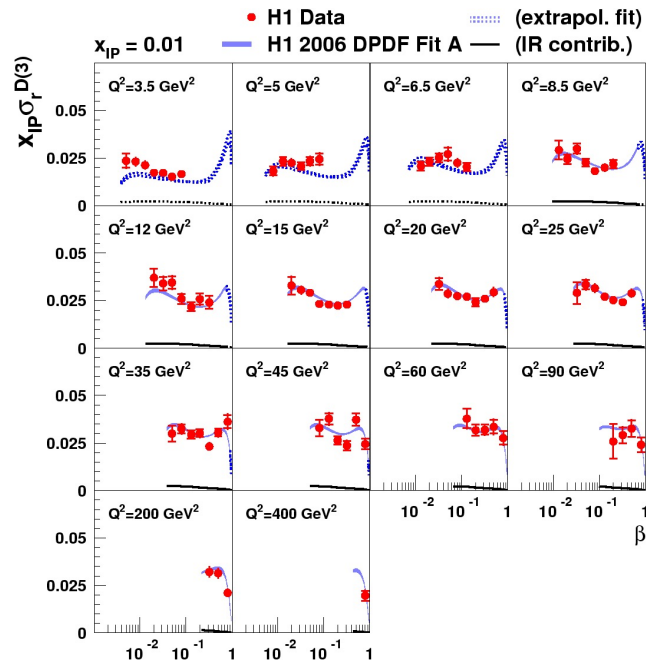
Leading twist
and ~10% of
total x-sec



Sensitivity to Diffractive Quarks & Gluons

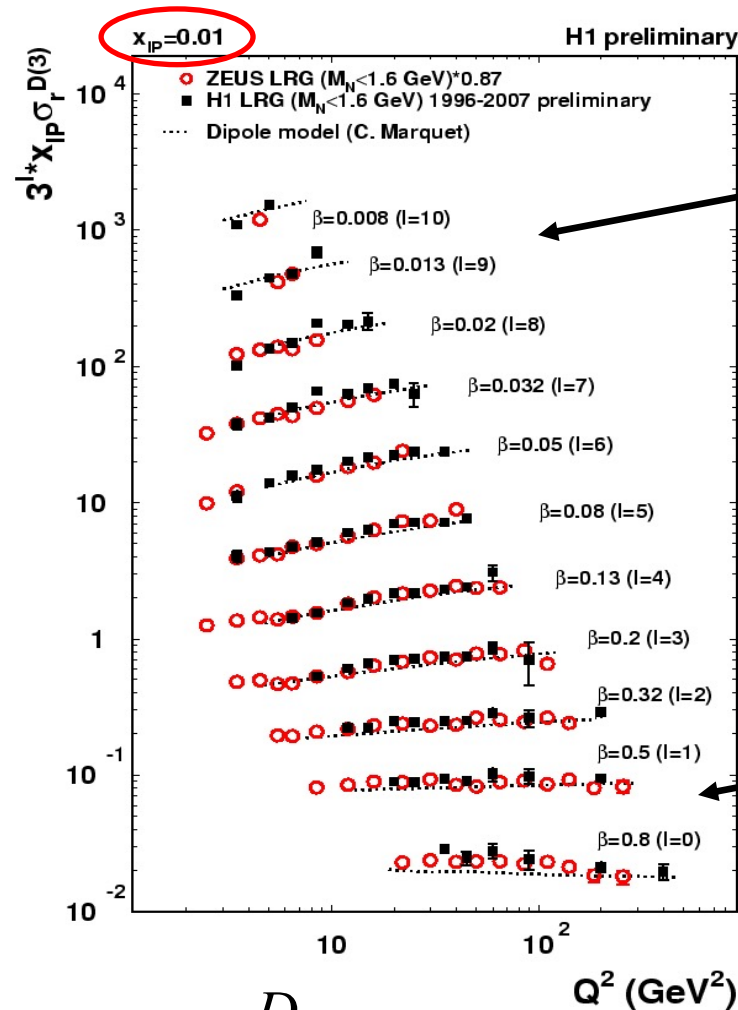


Similarly to
Inclusive DIS ...



Diffractive cross section
measures quark density

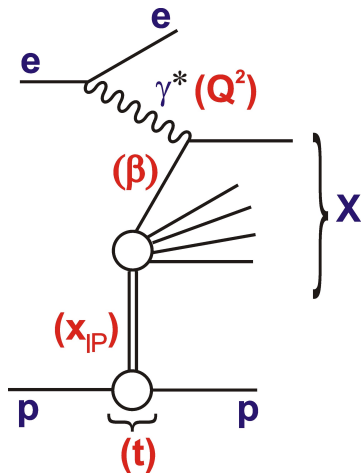
$$F_2^D = \sum_q e_q^2 \beta (q + \bar{q})$$



Q^2 dependence
tells us gluon
density via
DGLAP eqns

$$\frac{d\sigma_r^D}{d\ln Q^2} \sim \frac{\alpha_s}{2\pi} \left[P_{qg} \otimes g + P_{qq} \otimes q \right]$$

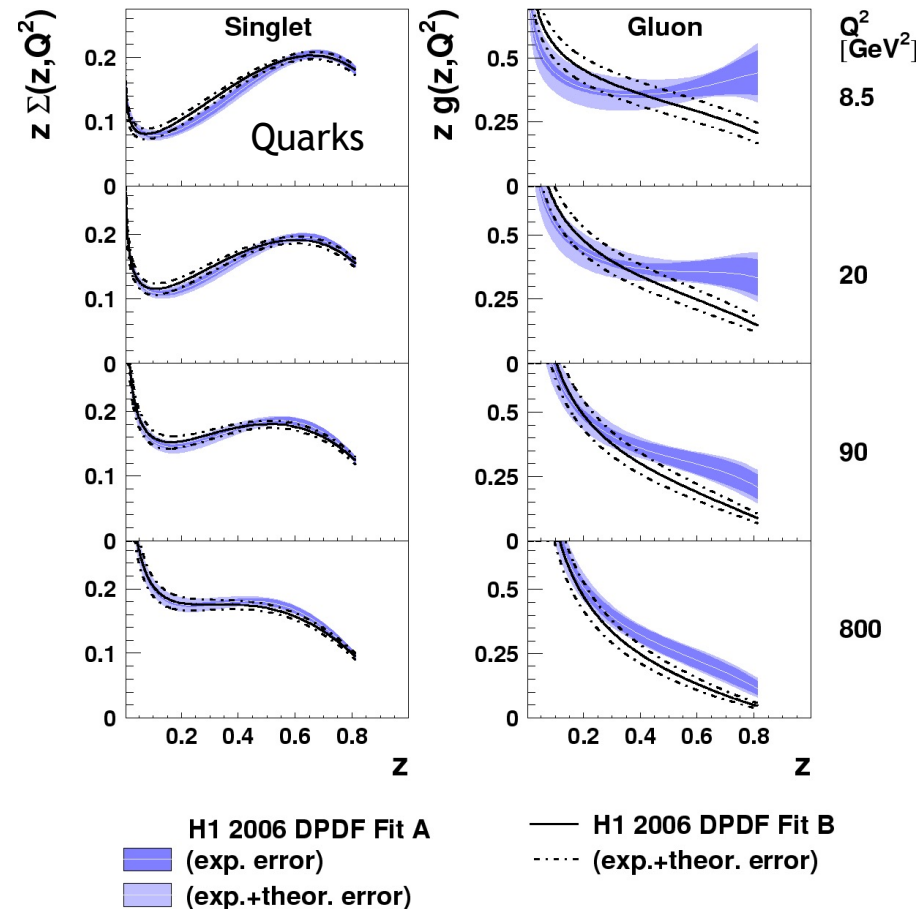
Diffractive Parton Densities (DPDFs)



DPDFs extracted through fits to inclusive (& jet) data, assuming NLO/NNLO DGLAP evolution, similarly to inclusive DIS

... dominated by gluon density extending to large momentum fractions, z

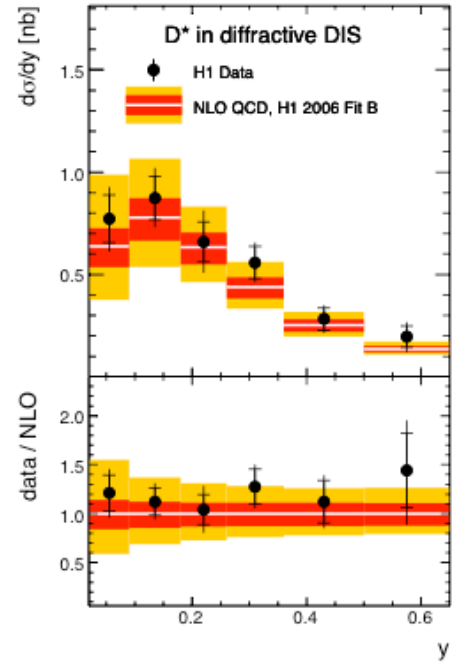
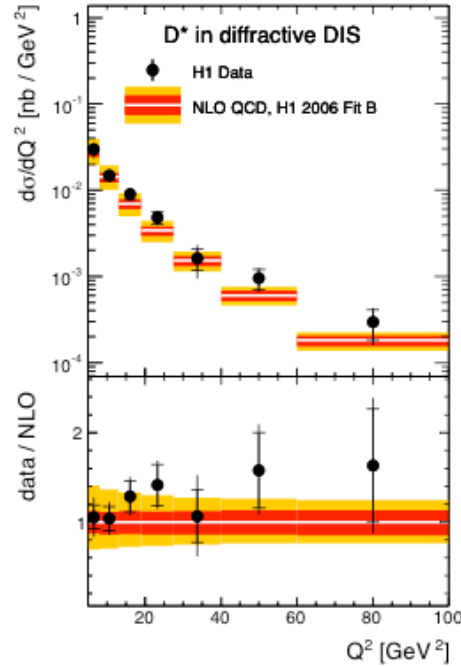
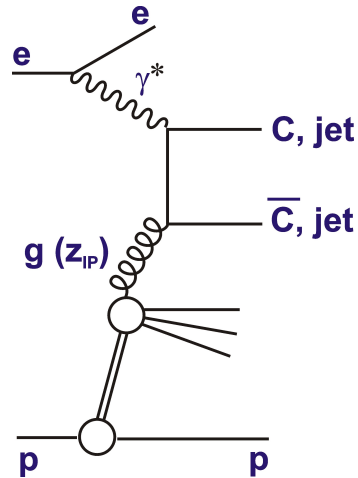
e.g. H1



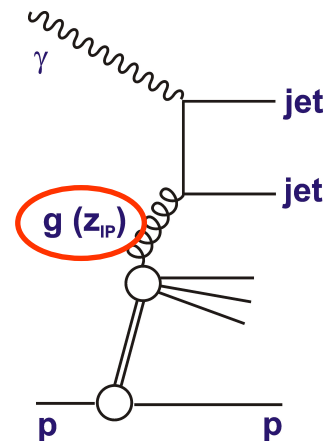
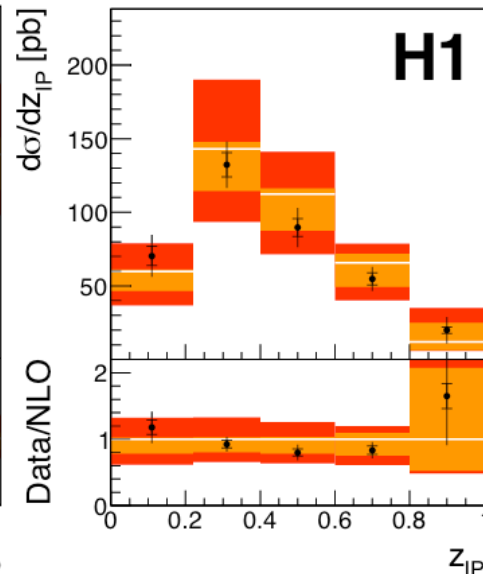
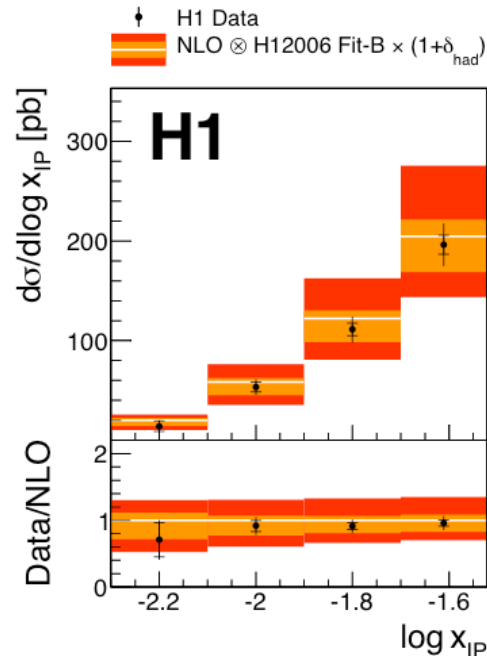
- NLO DGLAP QCD fits describe data over most of phase space
- Failure of diffractive PDF fits to describe data at lowest Q^2 ...

Testing Factorisation; eg HERA Jets & Charm

Remarkably good description of all variables in Diffractive DIS over a wide kinematic range



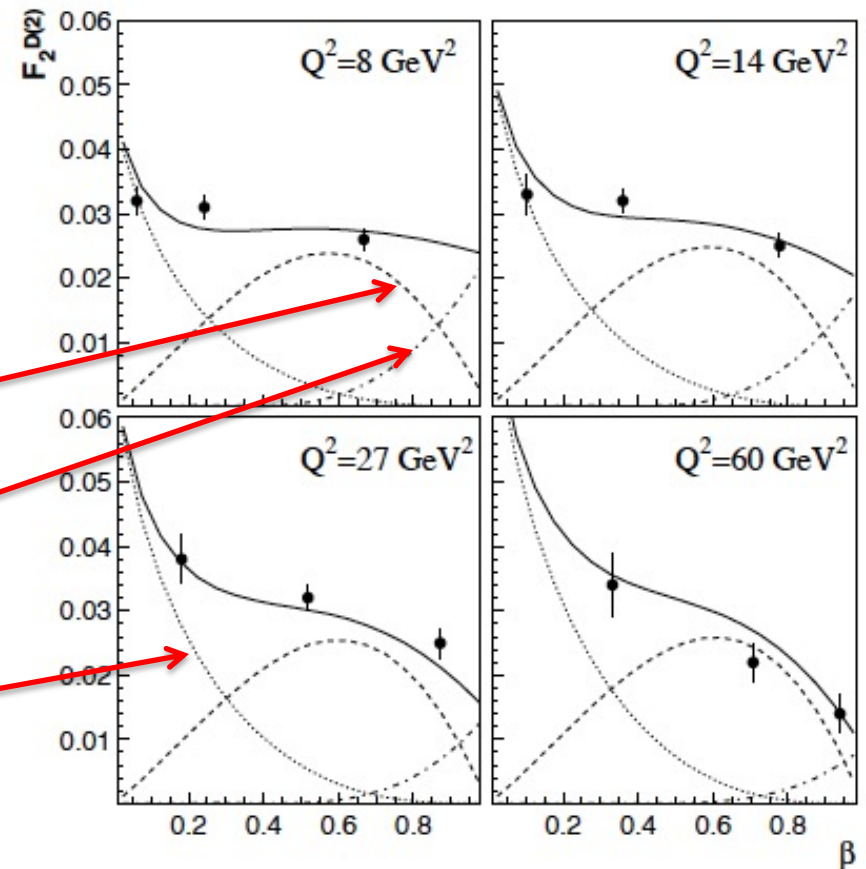
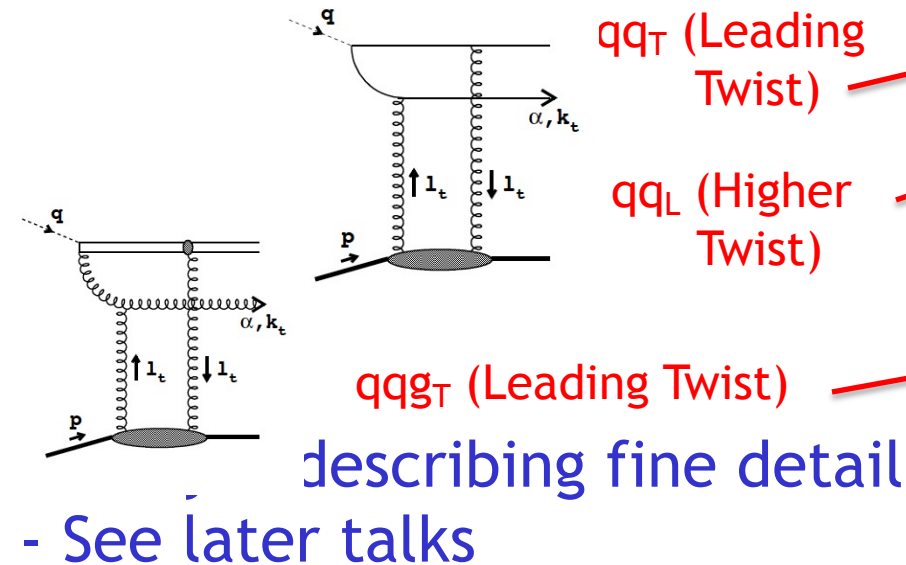
Charm in DIS



Dijets in DIS

Diffractive DIS & Dipole Models

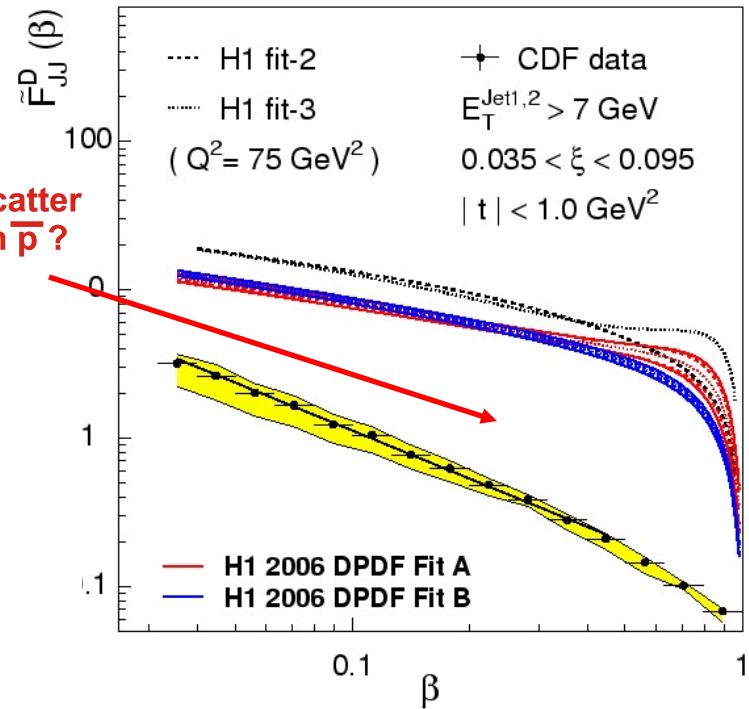
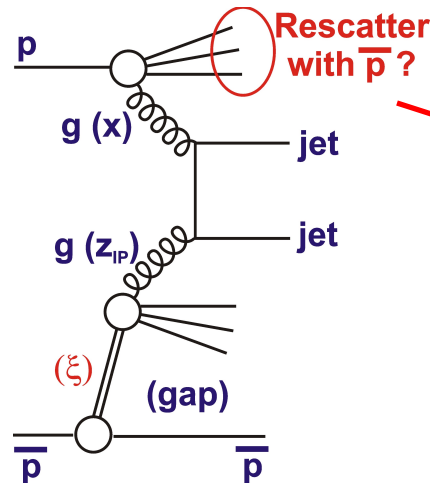
- Quality of H1 & ZEUS DPDF fits degrades at low $Q^2 < \sim 5 \text{ GeV}^2$
... low Q^2 breakdown of pure Leading Twist DGLAP approach
- Dipole models also applied,
but need $q\bar{q}$ -g terms (and
perhaps higher Fock states)



- See later talks

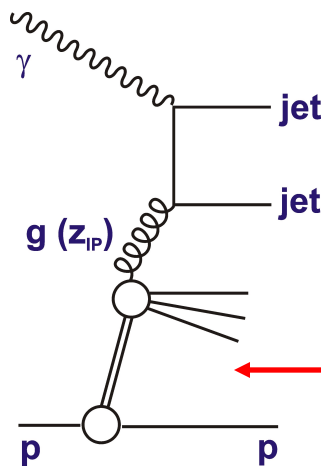
.. meanwhile in pp(bar) ...

Strong evidence for absorptive effects in comparing Tevatron diffractive dijets with HERA DPDFs ...
 `rapidity gap survival probability' $S^2 \sim 0.1$



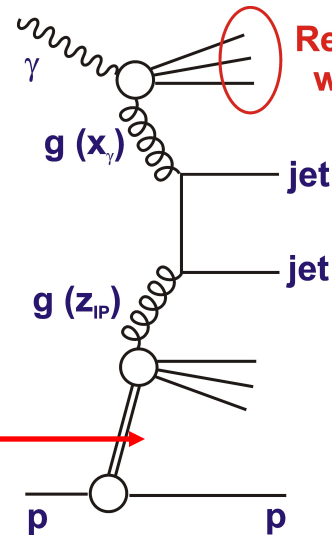
... photoproduction jets as the perfect control experiment?...

“Direct”
photon
 $(x_\gamma \rightarrow 1)$



“ $S^2 = 1$ ”

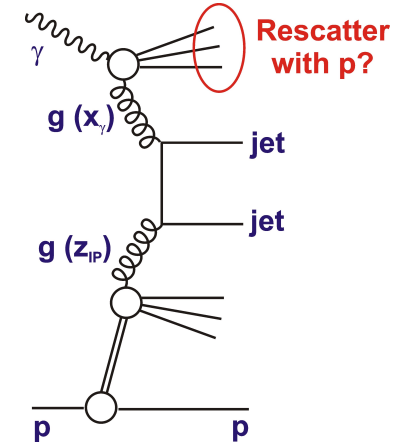
“Resolved”
photon
 $(x_\gamma < 1)$



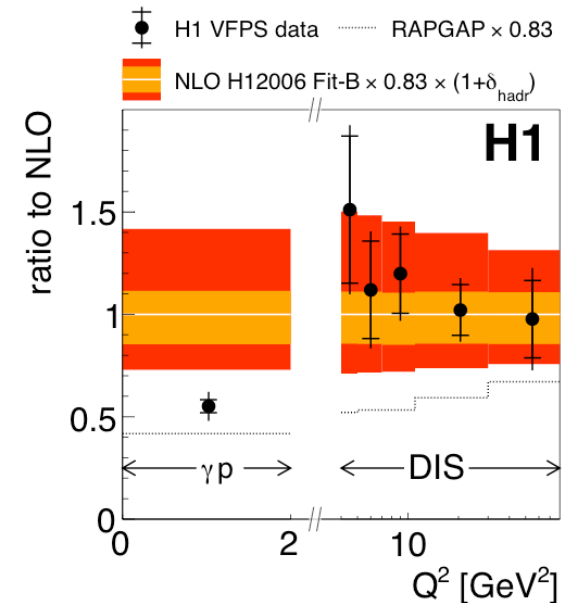
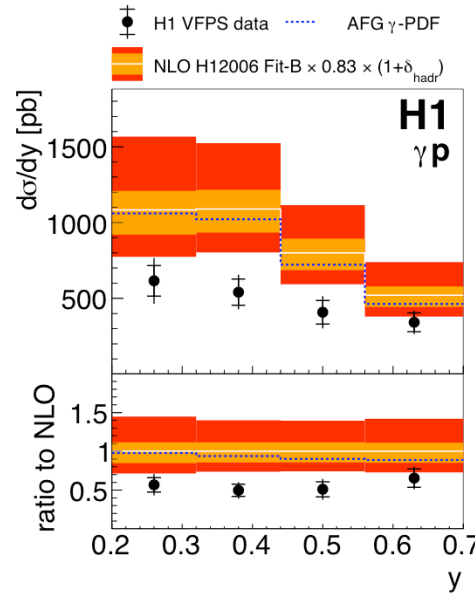
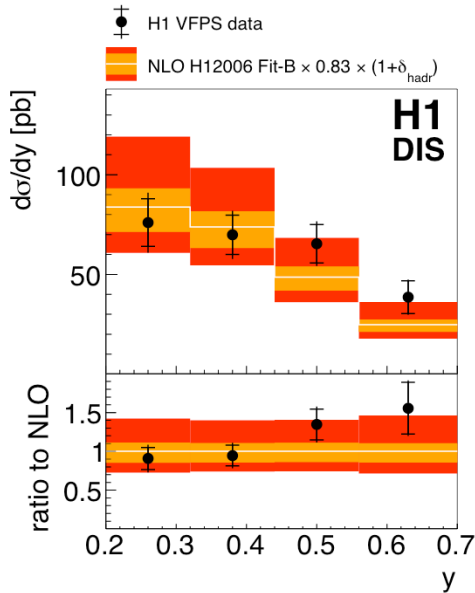
$S^2 ?$

GAP

Rapidity Gap Survival Probability in Diffractive Dijet Photoproduction



Data v NLO QCD
with H1 2006
Fit B DPDFs



From double ratio:

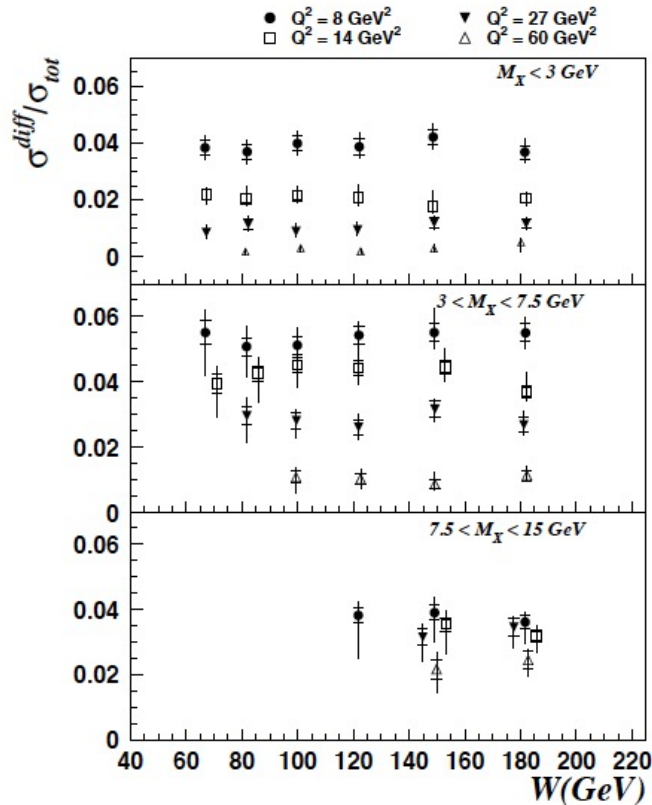
$$(\text{data/theory}) (\gamma p / \text{DIS}) = 0.51 \pm 0.09$$

- Gap survival unexpectedly has little dependence on x_γ
- Some inconsistencies between ZEUS and H1
→ mysteries still to be understood

Diffraction and the Electron-Ion Collider

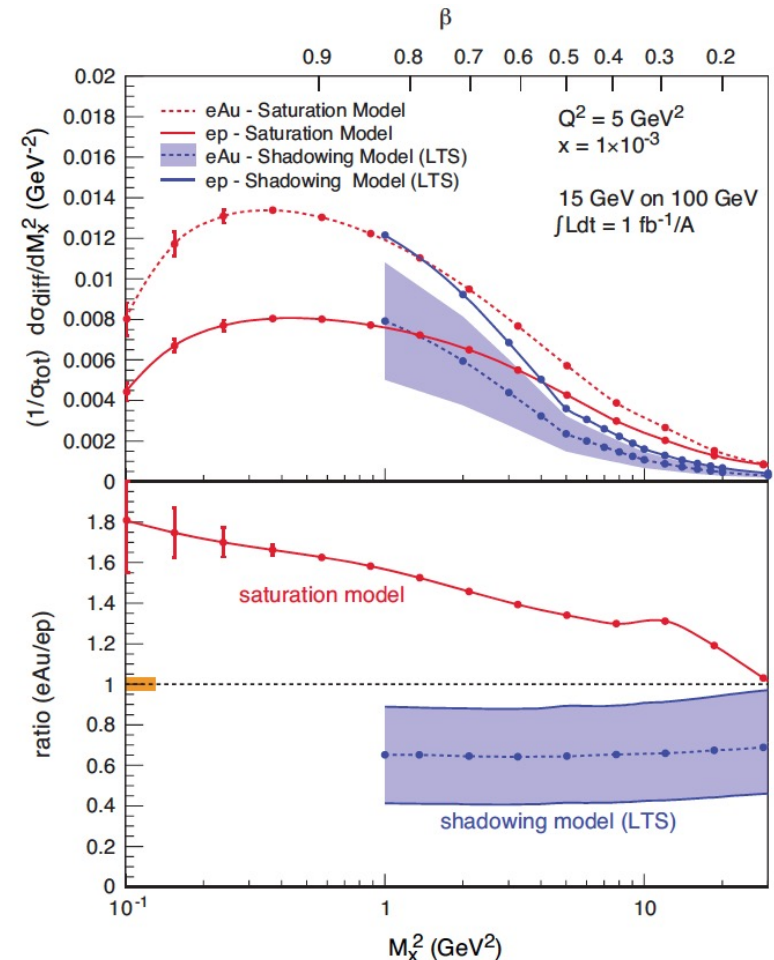
[Examples from some early studies]

'Day 1' at EIC: Diffractive / Inclusive Ratio



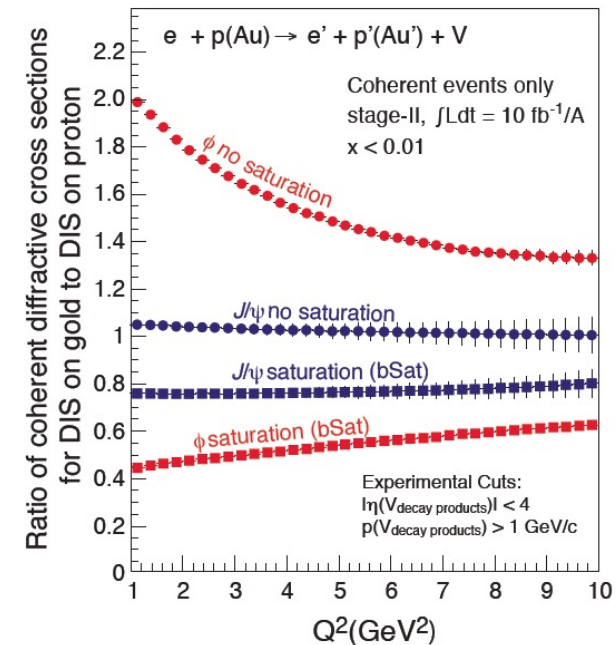
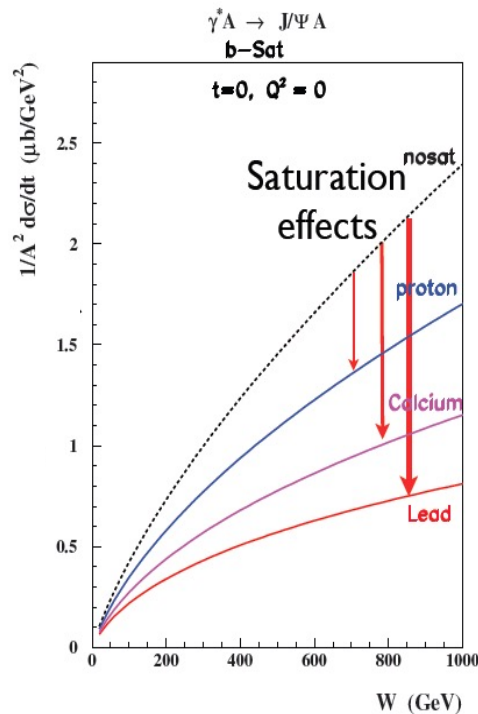
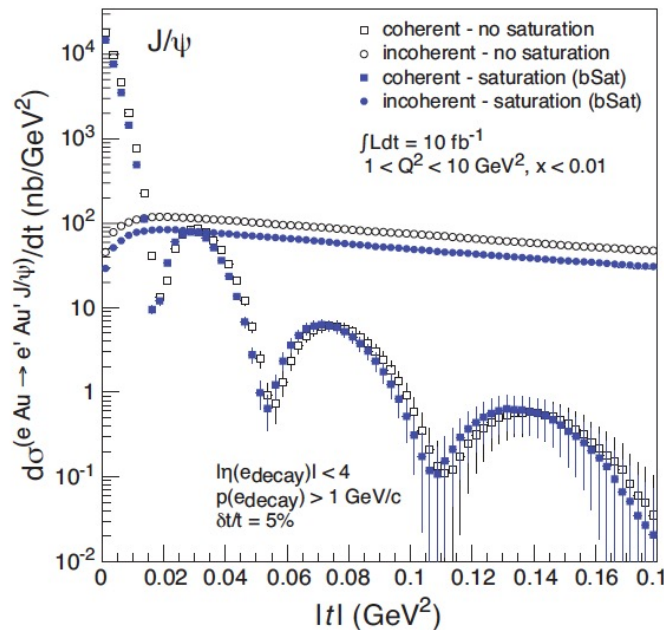
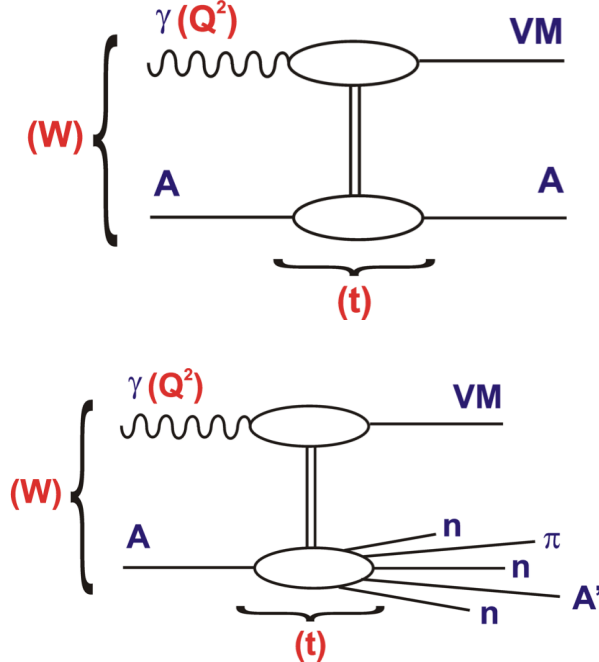
- Famous ZEUS plot ... Rather flat diffractive/inclusive ratio v x at fixed Q^2 , taken as evidence for saturation

- EIC 'Day 1' simulations confirm the importance of this sort of observable to disentangle saturation and shadowing ...
... increasing diff/incl ratio with A in saturation case ...

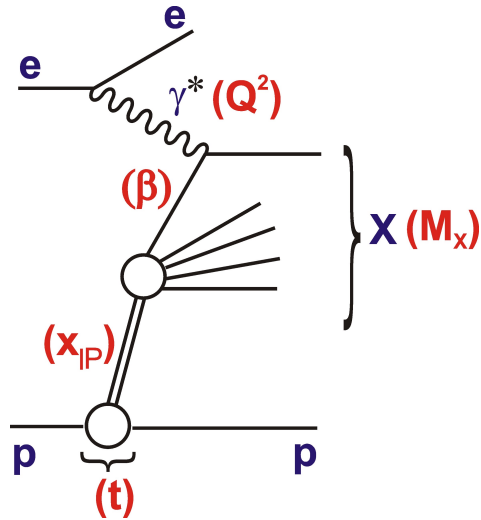


Exclusive Diffraction in eA

- Separation of coherent / incoherent can be done based on ZDC
- Opportunity to image structure
- Significant saturation effects predicted in coherent case ($eA \rightarrow eVA$), visible in total cross sections, A and t dependences
- ϕ mesons may be most sensitive

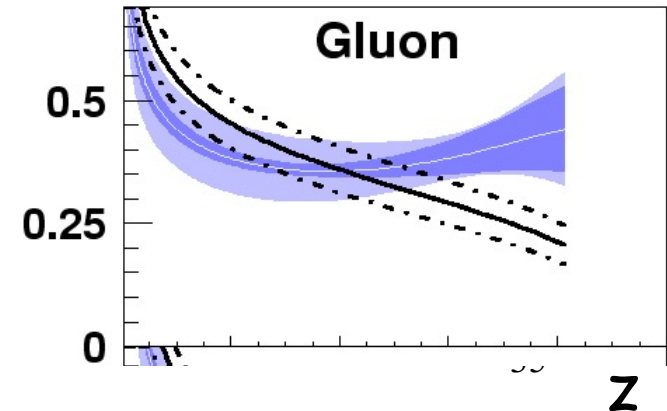
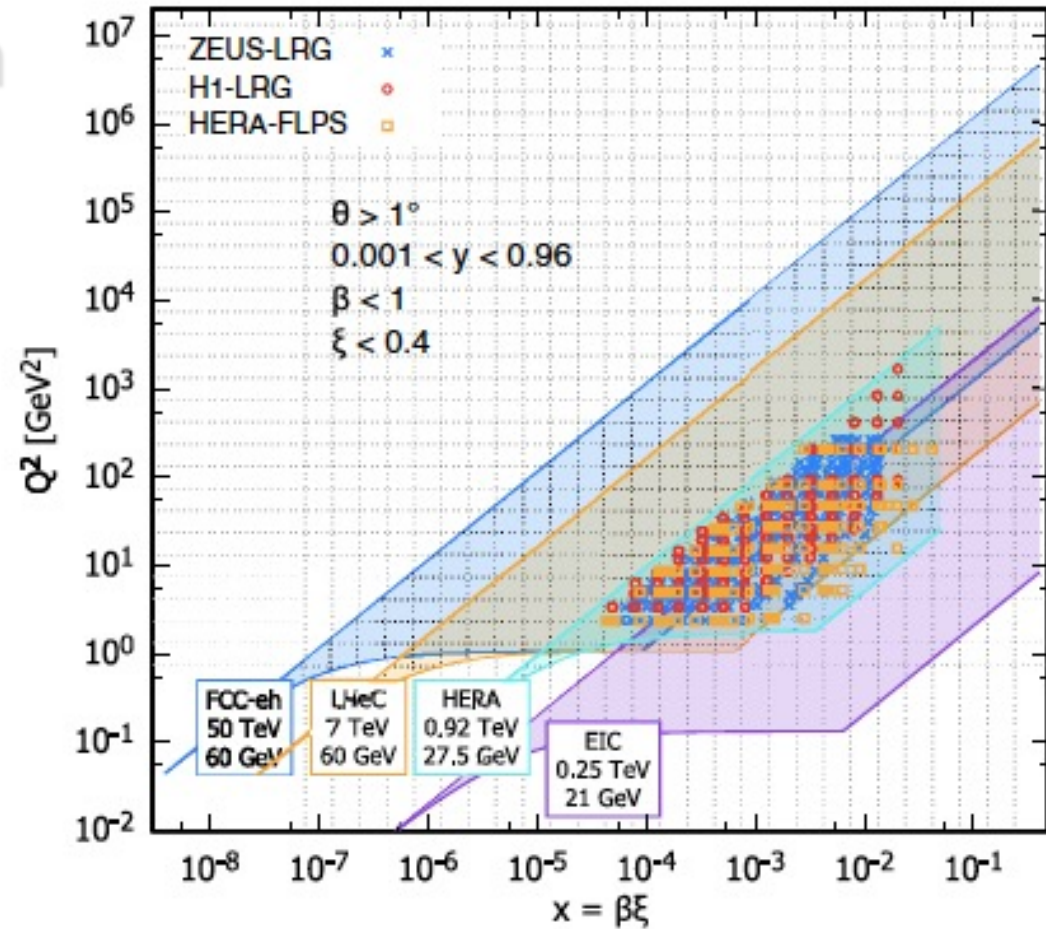


Inclusive Diffraction at EIC

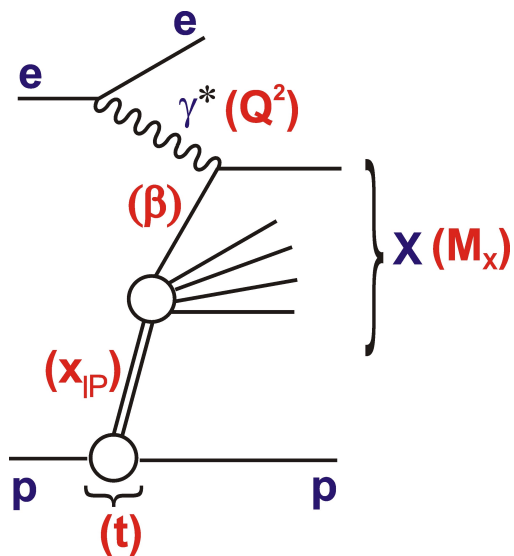


Lower centre of mass energy than HERA, but ...

- Fills gap in kinematic plane at large x (there are no fixed target data)
→ Sensitivity to poorly constrained structure at large momentum fraction (β or z)
- Inclusive diffraction has never been studied with nuclear or polarised targets



Inclusive Diffraction in ep at EIC: Scattered proton kinematics

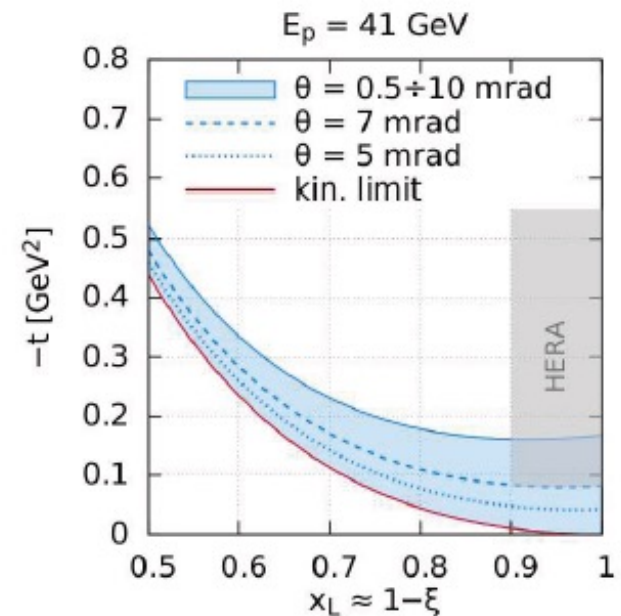
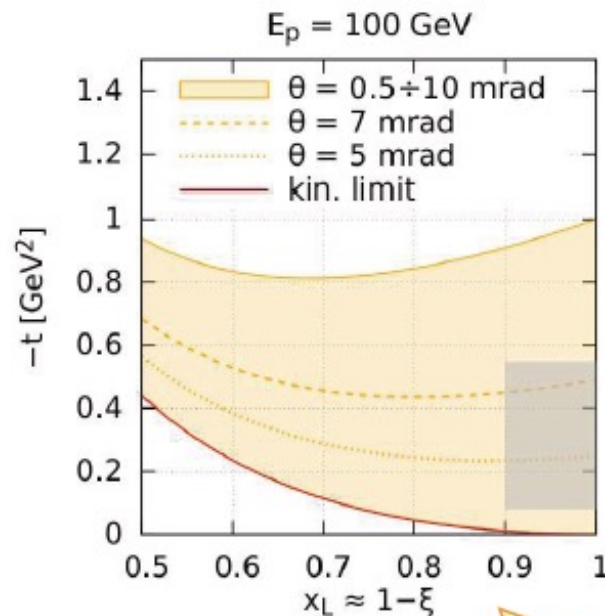
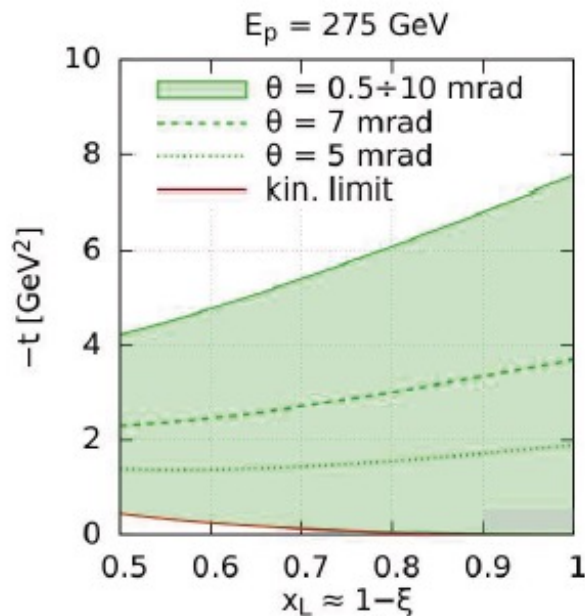


$$t \approx -p_T^2$$

$$x_L = \frac{E'_p}{E_p} = 1 - x_{IP}$$

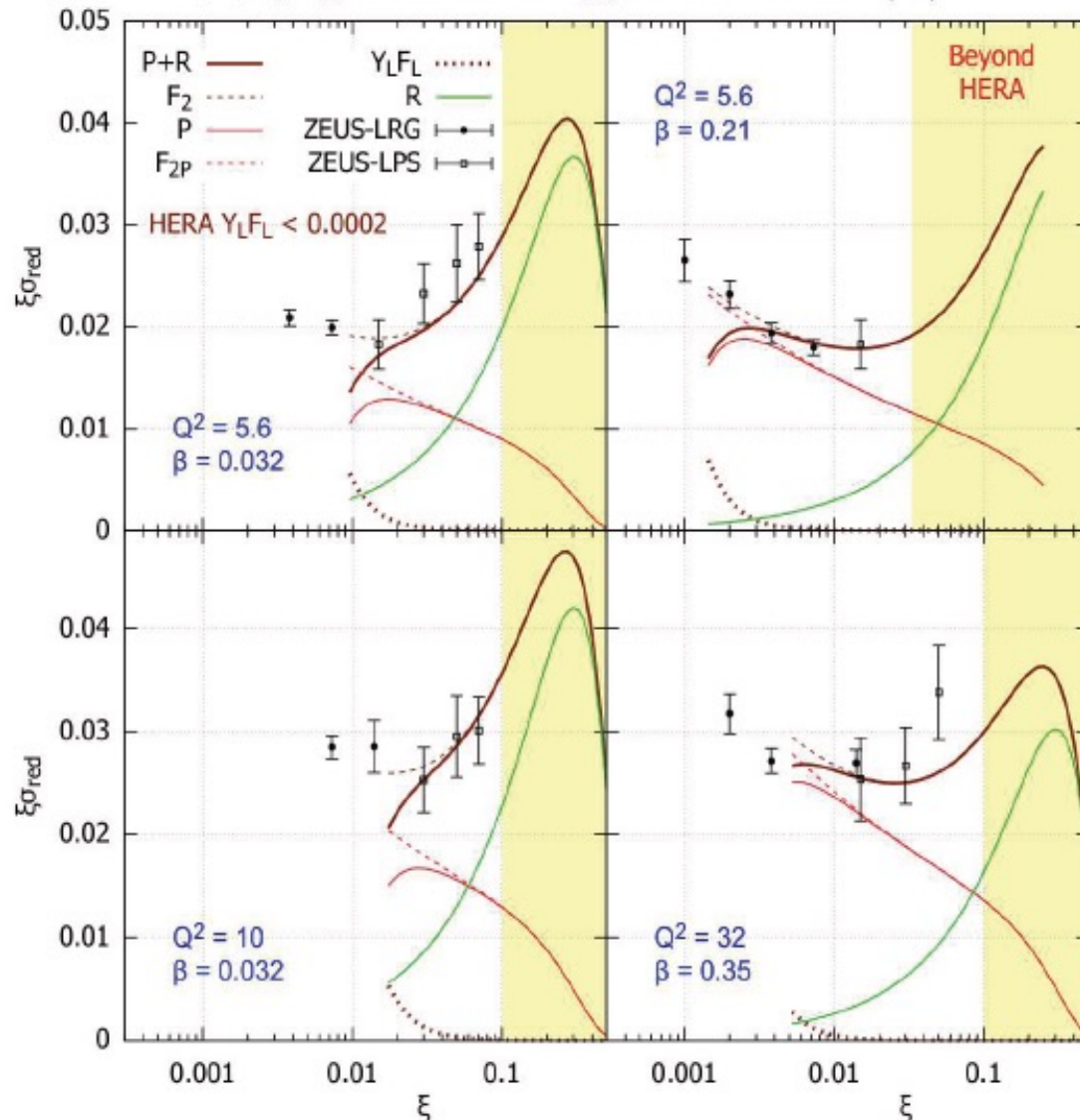
Planned EIC Roman pots provide:

- Good coverage in most interesting large x_L , low $|t|$, diffractive region for all $\sqrt{s}$
- Interesting coverage at smaller x_L at large $\sqrt{s}$ (sub-leading 'Reggeon' exchanges)



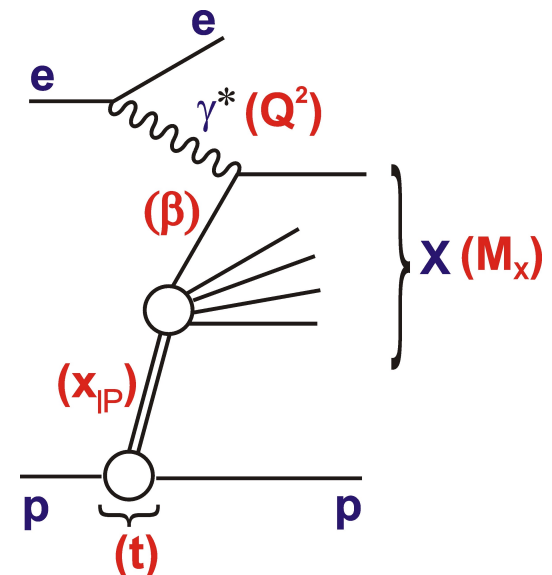
Inclusive Diffraction in ep at EIC: Sensitivity to sub-leading (non-pomeron) exchange

P, R, F_2 , F_L contributions to σ_{red} for 275×18 GeV (SJ)



→ Yellow shaded region at large x_L is previously unexplored

→ Opportunity to understand sub-leading Reggeon (meson) exchanges and measure their structure

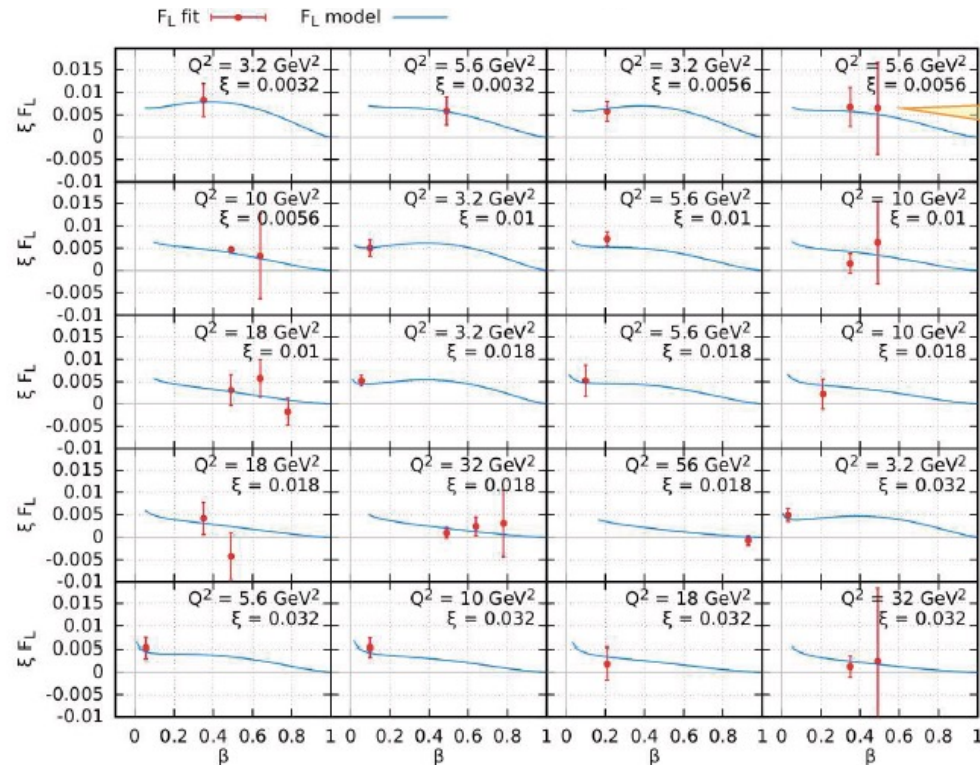
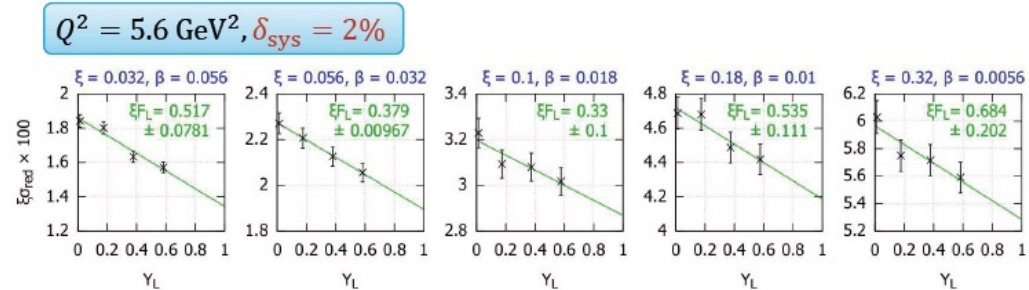


Inclusive Diffraction in ep at EIC: Sensitivity to diffractive longitudinal structure function

- Longitudinal structure function is proportional to gluon density at lowest order.
- Measurement at same (ξ, t, β, Q^2) and varying $\sqrt{s}$ (hence y) gives sensitivity to F_L^D (Rosenbluth plots)

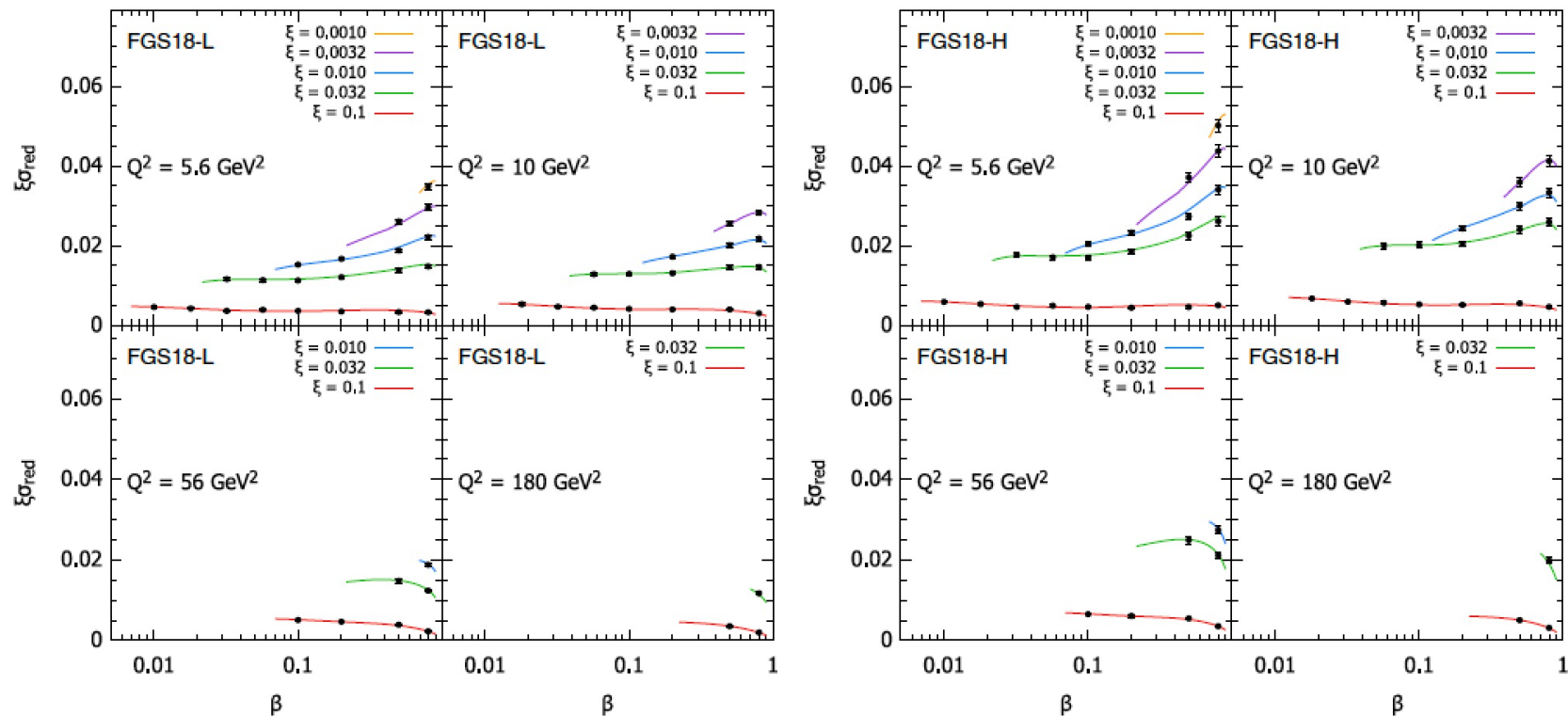
$$\sigma_{\text{red}}^D = F_2^D - \frac{y^2}{1 + (1 - y)^2} F_L^D$$

- First simulations look promising
- Precision strongly dependent on correlations between systematics at different $\sqrt{s}$



Inclusive Diffraction from Nuclei at EIC: Selected Simulated Data for $e \text{ Au} \rightarrow e X \text{ Au}$

- Inclusive diffraction from nuclei never previously studied
- Comparing eA / ep may reveal non-linear (satur'n) dynamics



Simulations based on different versions of FGS model →

- illustrates accessible kinematic range and ability to distinguish between (widely varying) models

Summary

HERA revolutionised our understanding of Diffraction in QCD

Exclusive (vector meson) processes ($ep \rightarrow eVp$):

- Turn-on of hard scales mapped for multiple VM species.
- $(Q^2 + M_V^2)/4$ is often a good scale choice for comparisons
- Hard VM production in principle sensitive to proton gluon density / saturation

Inclusive process ($ep \rightarrow eXp$):

- Dominant contribution can be viewed as LT DIS off ‘soft’ colour-singlet exchange: properties similar to the ‘soft pomeron’
- Colour Singlet Exchange dominated by gluons carrying large momentum fraction

EIC will go further with improved beamline instrumentation, much larger luminosity, ep/eA comparisons and polarisation

→ 3D imaging

→ High density effects